

# Evaluation of measurement results

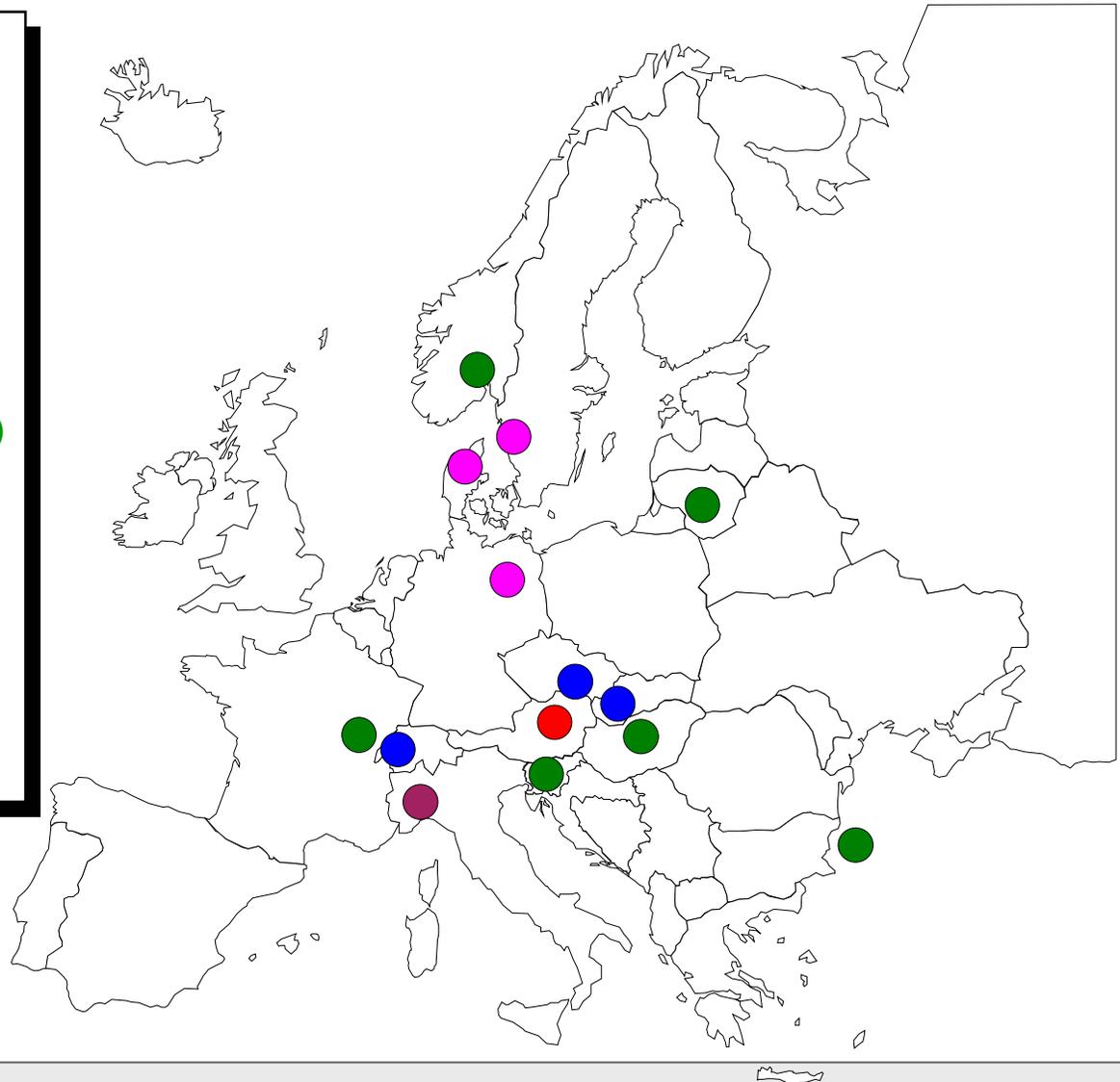
Start of the project in spring 2002

<b>PROPOSED EUROMET PROJECT</b>	
1. Ref. No: (please leave blank)	2. Subject Field: <b>water flow</b>
3. Type of collaboration: <b>Interlaboratory comparison</b>	
4A: Partners: <b>BEV, OMH, PTB, SP, UME, CMI, METAS, CETIAT</b> (BNM), SMU, DTI, LEI, MIRS, YUSTERVESENET (institutions)	4B: CEC funded? no
5. Participating countries: <b>AT, H, D, S, TR, CZ, CH, FR, SK, DK, LI, SI, N</b>	
6. Title: <b>Intercomparison of two electromagnetic meters DN 25</b>	
7. Description:  0 This project shall compare the test facilities of NMIs by means of two electromagnetic meters for water, DN 25, as a robin round test. The comparison shall be performed at a temperature of 50 °C, pressure approximately 1 bar, flow range: 1 m <sup>3</sup> /h to 10 m <sup>3</sup> /h, test mode: preferably dynamic measurement.  For further details see enclosure.  Prior to the robin round test the meters are endurance tested at the BEV for long time stability and repeatability.  For the evaluation of the test results, among others, a Youden-plot is foreseen.  Subsequently to this EUROMET project the comparison will be extended to some test laboratories (verification laboratories) at first in Austria and also in Germany.	
8. Additional remarks: For the setup of a final schedule the interested laboratories are requested to confirm their participation.  OMH, PTB/ Institute Berlin and SP have already agreed to join the project!	
9. Proposer's name: <b>Prof. Dr. Franz Adunka</b> Address: <b>BEV, Arltgasse 35, A-1160 Wien,</b> Austria  Telephone: <b>++43 1 49 110 537</b> Fax: <b>++43 1 49 20 875</b> e-mail: <b>F.Adunka@metrologie.at</b>	

## Participating institutes in Europe

- Austria (BEV)-pilot lab
- Slovakia (SMU)
- Czech republik (CMI)
- Switzerland (METAS)
- Austria (BEV, 9. 2002)
- Sweden (SP)
- Denmark (DTI)
- Germany (PTB-Berlin)
- Austria (BEV, 1. 2003)
- Slovenia (JP Energetika)
- France (CETIAT)
- Norway (Justervesenet)
- Turkey (UME)
- Hungary (OMH)
- Lithuania
- Austria (BEV, 12. 2003)
- Italy
- Austria (BEV, 2. 2004)

blue ... 1st cycle  
 violett ... 2nd cycle  
 green ... 3rd cycle  
 brown ... 4rd cycle



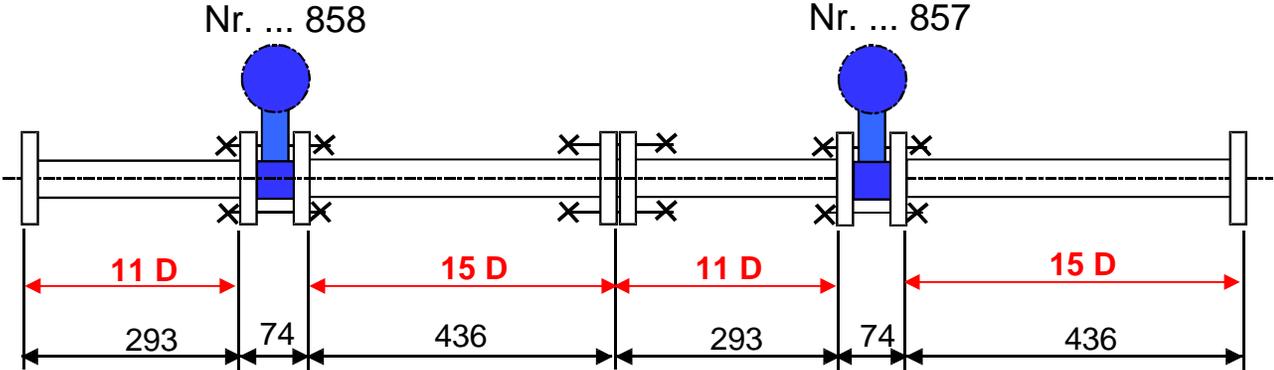
## Details

### Significant data

- Medium: water
- Pressure: <1 bar downstream of the second meter  
(reference value: 0,6 bar)
- Temperature: 50 °C
- Flow range:  $1.000 \text{ L/h} \leq Q \leq 10.000 \text{ L/h}$
- ◆ pipe diameter: DN 25

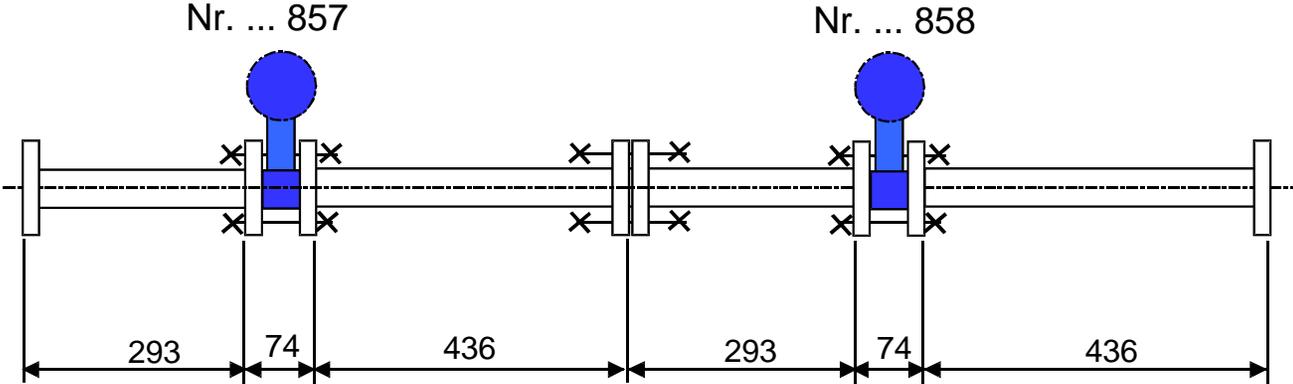
# Sketch of the arrangement of meters under test

← flow direction



Arrangement 1

← flow direction



Arrangement 2

## Test conditions

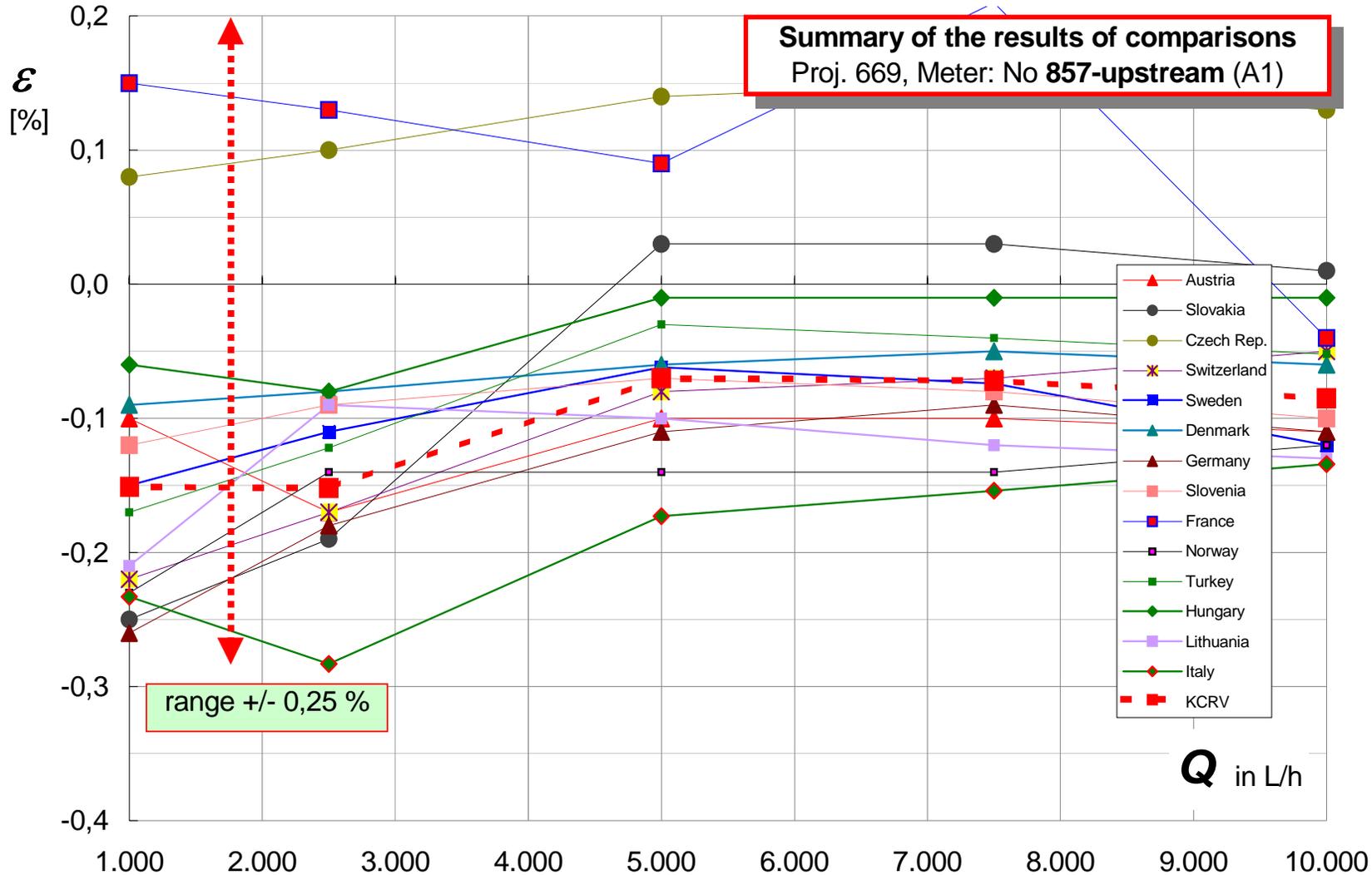
flow rate	number of repeated measurements	Volume at the tests	temperature	pressure at the outlet
L/h	N		°C	bar
10000	≥ 10	depending of the test rig	(50 ± 0,5)	ca. 0,6
7500				
5000				
2500				
1000				

**meter, straightener, transport box**

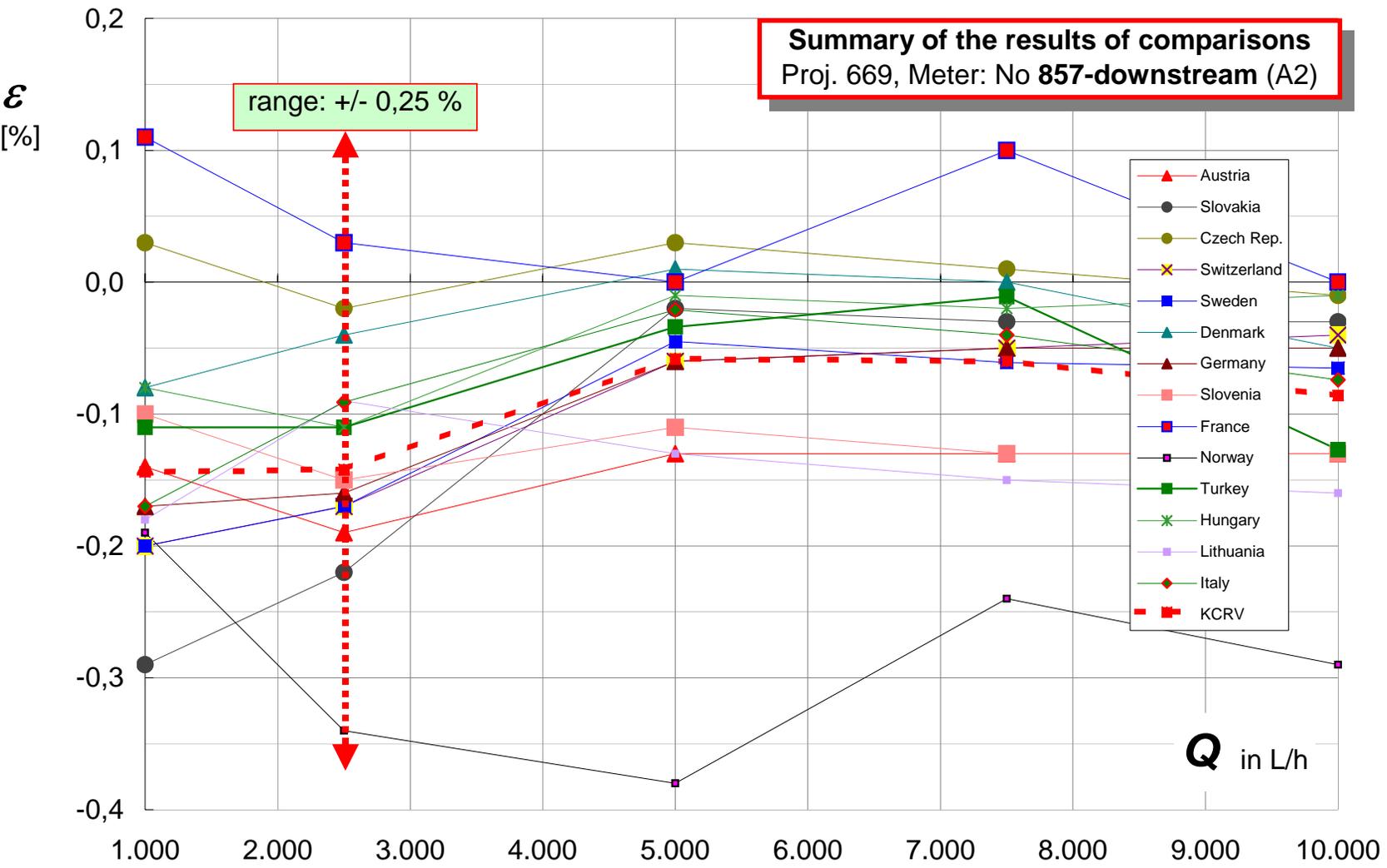


# **EUROMET comparison**

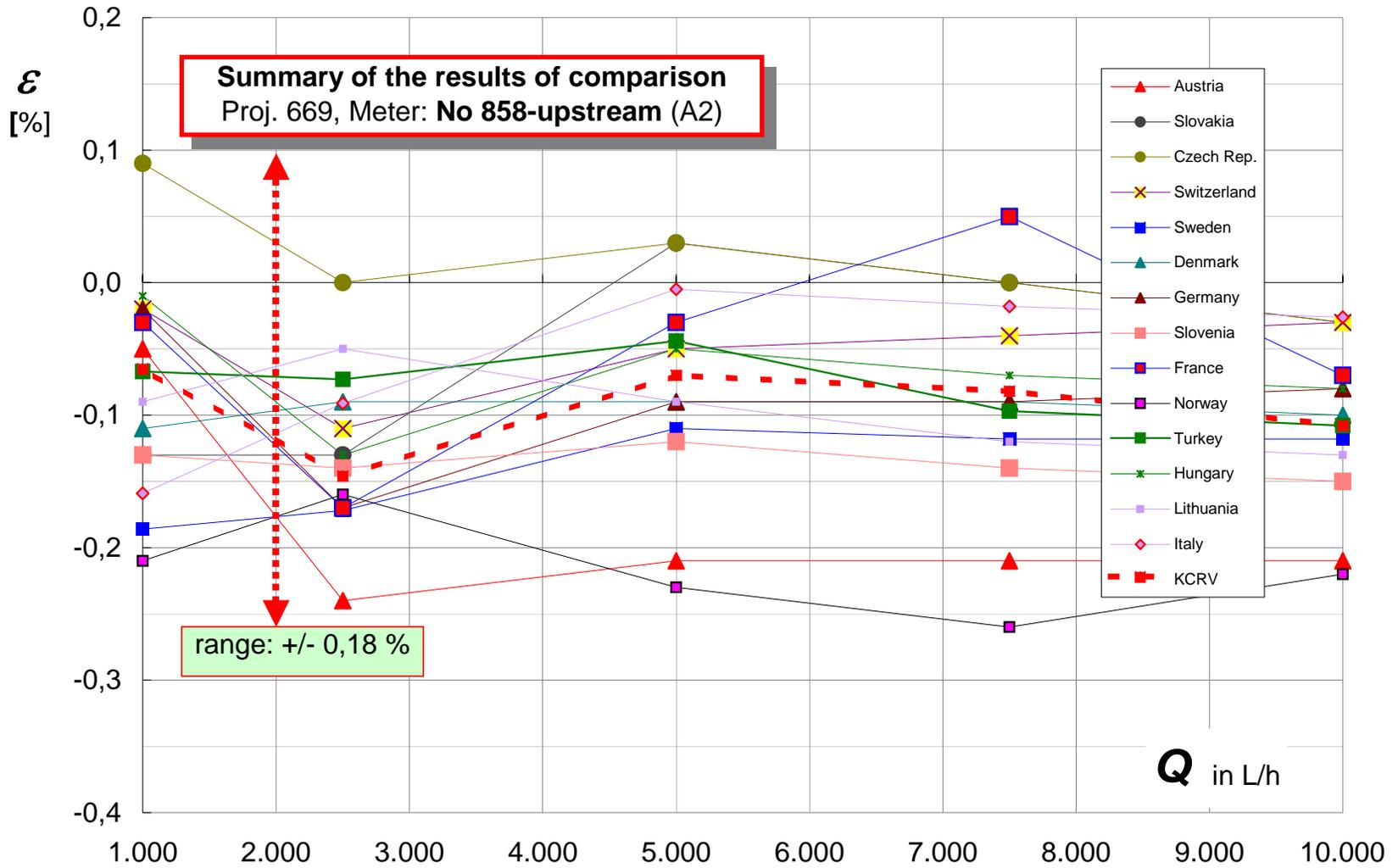
# Results of the EUROMET proj. 669 ... 857 upstream



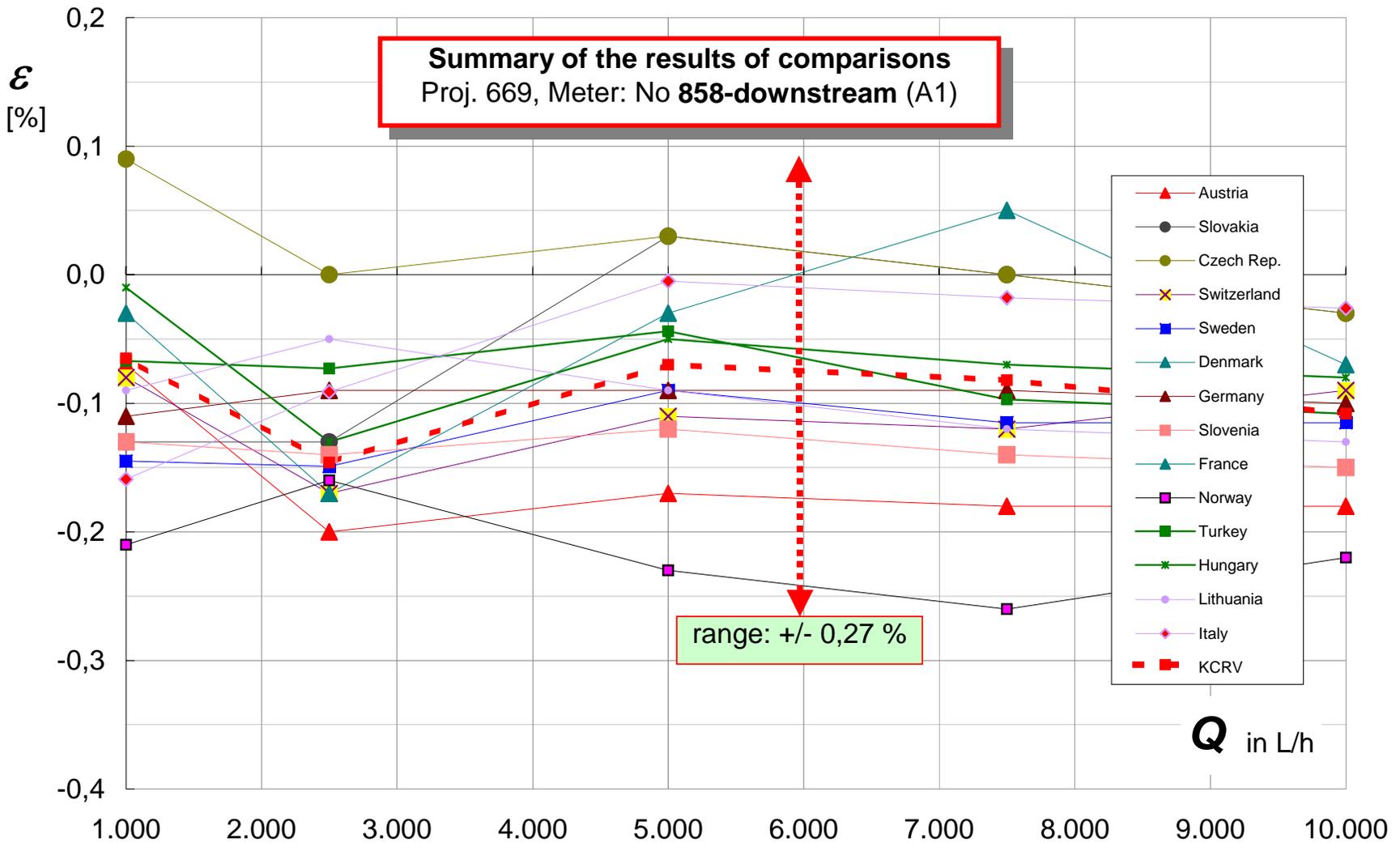
# Results of the EUROMET proj. 669 ... 857 downstream



**Results of the EUROMET proj. 669 ... 858 upstream**

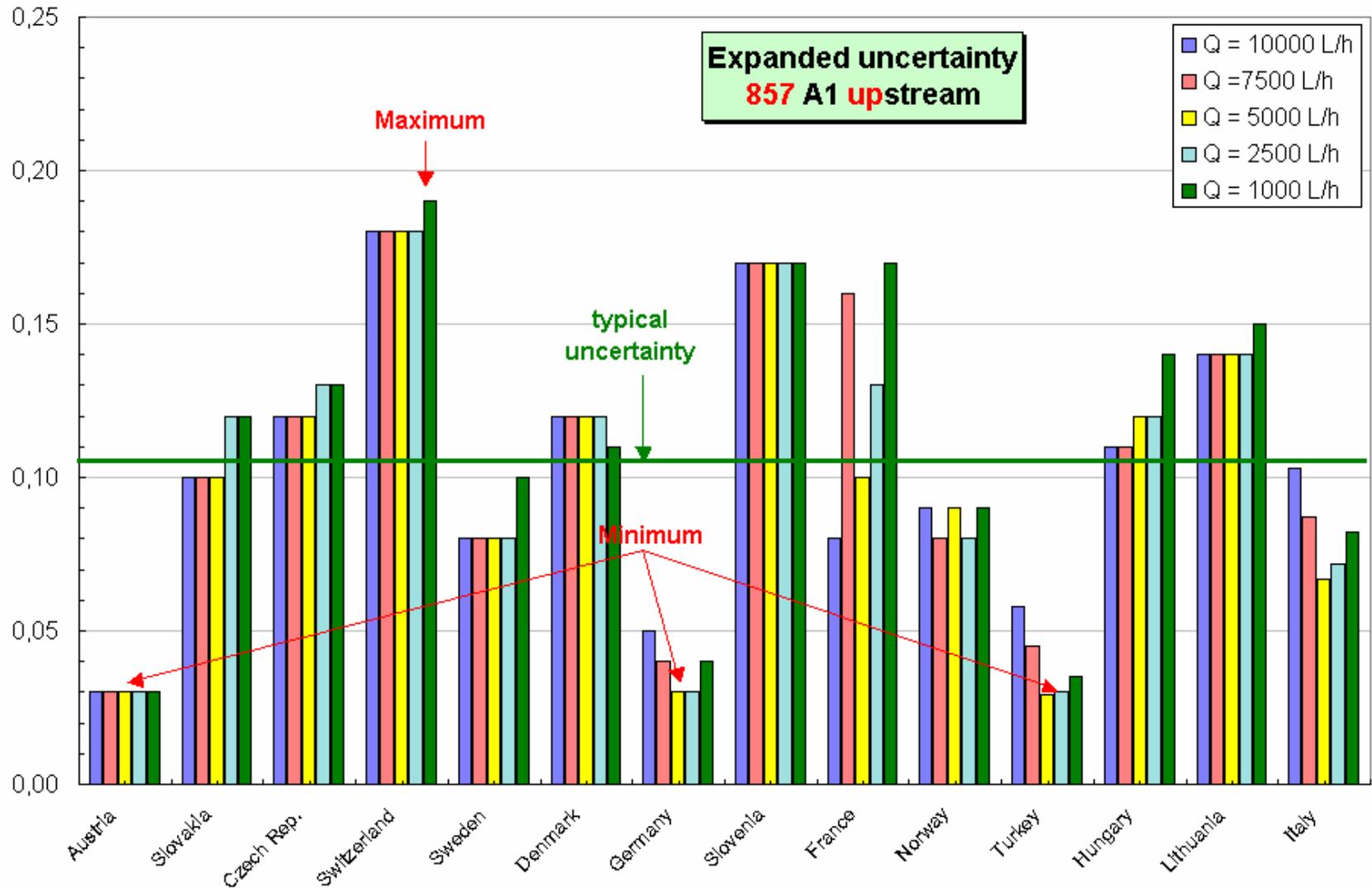


# Results of the EUROMET proj. 669 ... 858 downstream

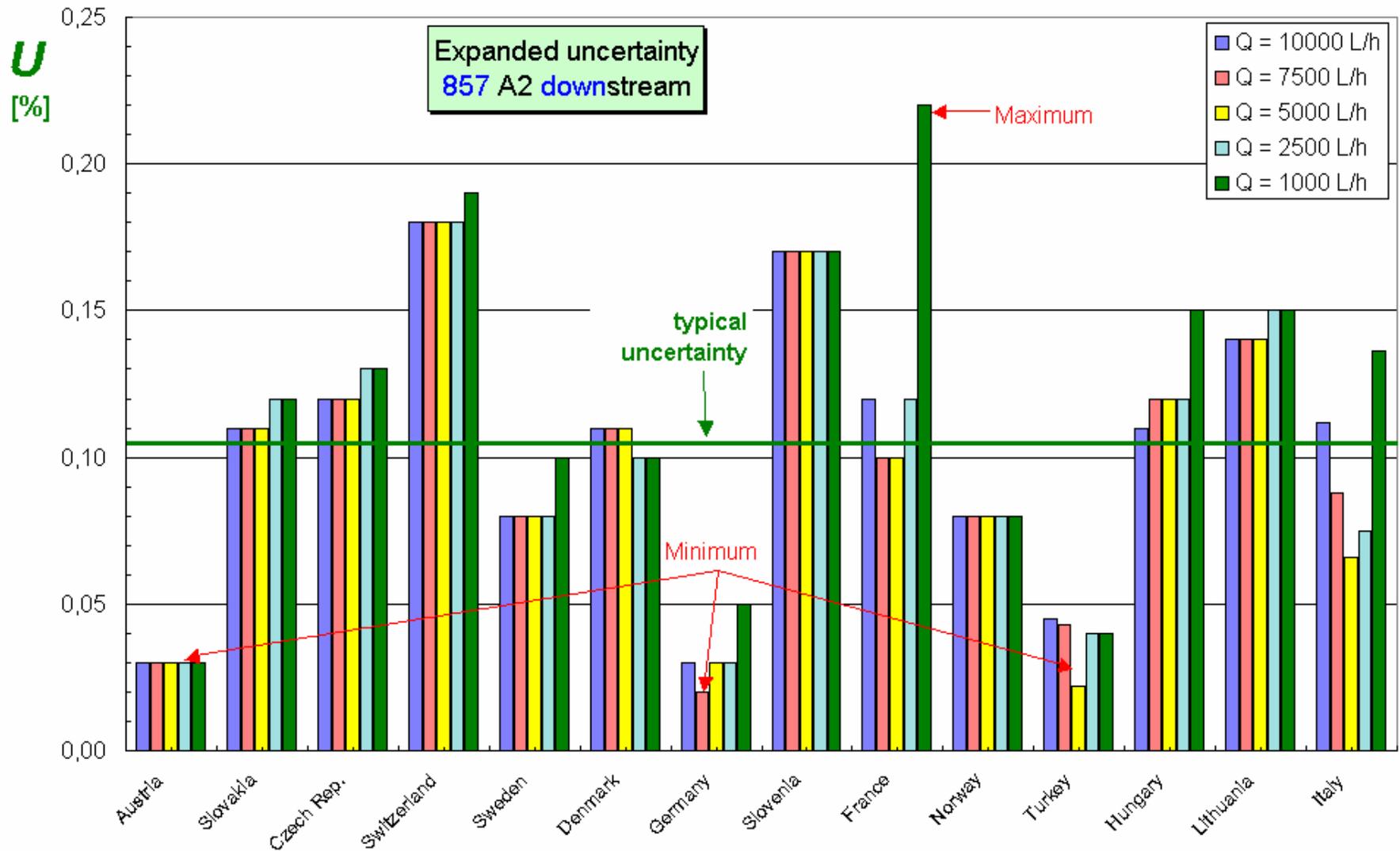


# Uncertainties 857 A1 upstream

**U**  
[%]

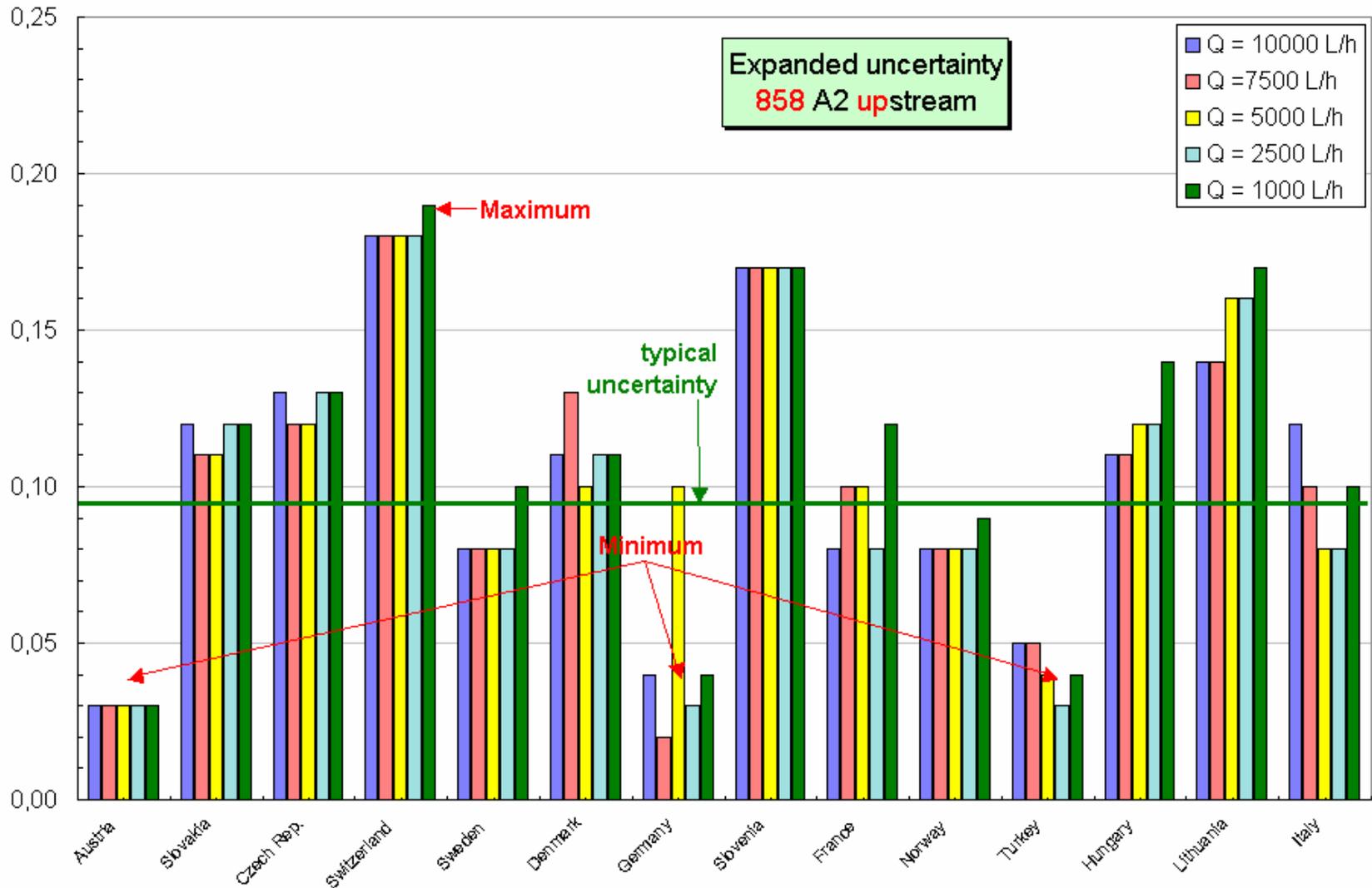


**Uncertainties 857 A2 downstream**

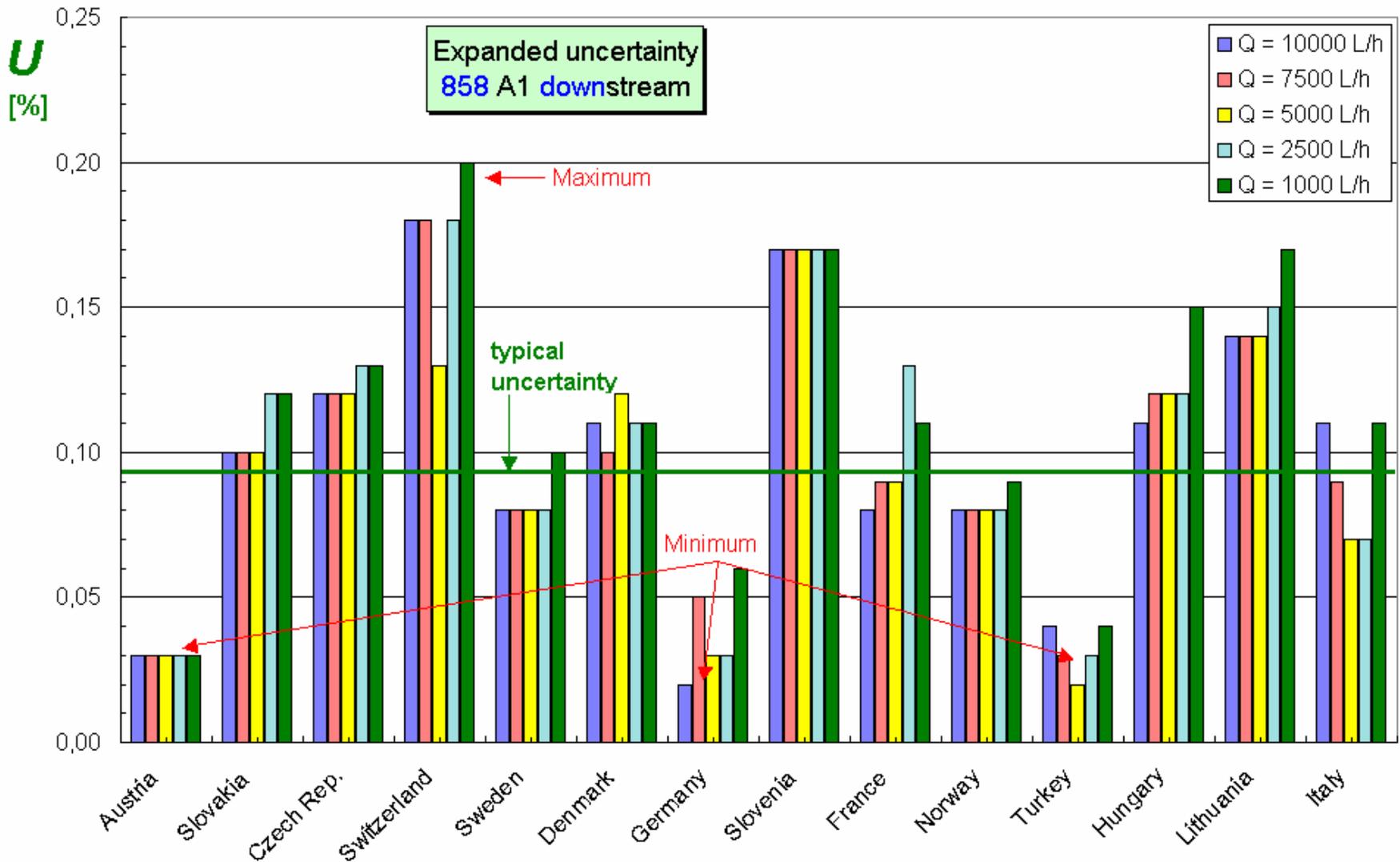


# Uncertainties 858 A2 upstream

**U**  
[%]



**Uncertainties 858 A1 downstream**



## Test to get the KCRV: $\chi^2$ -Test

## What do you do to get the best reference value ? - 1

What is the **referenz value (KCRV)** for all measurements ? → the **true value**, but nobody knows the true value. We search for the best estimation of the true value!! There are three methods

1<sup>st</sup> approach: the mean → it is the best approximation of the true value, if the measurements are normal distributed. We can evaluate the mean by the formula:

$$x_0 = \frac{1}{N} \sum_{i=1}^N x_i$$

2<sup>nd</sup> approach: to rate the measurements by their measurement uncertainty by the following formula

$$x_{0,B} = \frac{\sum_{i=1}^N p_i x_i}{\sum_{i=1}^N p_i} \quad \text{mit} \quad p_i = \frac{1}{u^2(x_i)}$$

**Statistic tests -  
for example: the  $\chi^2$ -Tests**

## Minimum $\chi^2$ -procedure

Situation: there are measurement results:  $(x_i, y_i, u(x_i))$

On the other hand: we have an unknown mathematical function  $F(x_i, \varepsilon_1, \varepsilon_2, \dots)$  with variable coefficients  $\varepsilon_1, \varepsilon_2 \dots$

We assume

$$\chi^2 = \sum_{i=1}^N \frac{(y_i - F(x_i, \varepsilon_1, \varepsilon_2, \dots))^2}{u^2(x_i)}$$

Proceeding: variation of the parameters  $\varepsilon_1, \varepsilon_2 \dots$  but  $\chi^2$  is a minimum!

**Chi-Quadrat-Test - nach Nielsen**

Procedure by **Nielsen**; reference value is doubtful by  $u^2(x_{ref})$ :

$$\chi_{obs}^2 = \frac{(x_1 - x_{ref})^2}{u^2(x_1) - u^2(x_{ref})} + \frac{(x_2 - x_{ref})^2}{u^2(x_2) - u^2(x_{ref})} + \frac{(x_3 - x_{ref})^2}{u^2(x_3) - u^2(x_{ref})} + \dots$$

$$\dots + \frac{(x_N - x_{ref})^2}{u^2(x_N) - u^2(x_{ref})}$$

We ask for the probability because  $\chi_{obs}^2$  and  $\chi^2(\nu)$  have the same distribution. Condition is:

$$P\{\chi^2(\nu) > \chi_{obs}^2\} > 5\%$$

Excel:

$$\text{chivert}(\chi_{obs}^2, \nu)$$

## Chi-Quadrat-Test by Cox and Nielsen

Procedure by **Cox**: reference value  $x_{ref}$  is in an interval of  $P \geq 5 \%$

$$\chi_{obs}^2 = \frac{(x_1 - x_{ref})^2}{u^2(x_1)} + \frac{(x_2 - x_{ref})^2}{u^2(x_2)} + \frac{(x_3 - x_{ref})^2}{u^2(x_3)} + \dots + \frac{(x_N - x_{ref})^2}{u^2(x_N)}$$

Procedure by **Nielsen**; reference value is uncertain by an interval of  $u(x_{ref})$ :

$$\chi_{obs}^2 = \frac{(x_1 - x_{ref})^2}{u^2(x_1) - u^2(x_{ref})} + \frac{(x_2 - x_{ref})^2}{u^2(x_2) - u^2(x_{ref})} + \frac{(x_3 - x_{ref})^2}{u^2(x_3) - u^2(x_{ref})} + \dots$$
$$\dots + \frac{(x_N - x_{ref})^2}{u^2(x_N) - u^2(x_{ref})}$$

## Chi-Quadrat-Test - nach Nielsen

We ask for the probability because  $\chi^2_{\text{obs}}$  and  $\chi^2(\nu)$  have the same distribution. Condition is:

$$P\{\chi^2(\nu) > \chi^2_{\text{obs}}\} > 5\%$$

Excel:

$$\text{chivert}(\chi^2_{\text{obs}}, \nu)$$

**Example: - 14 participants,  $\nu = 13$ , 857 downstream**

	reported values	abs deviation from mean	reported uncertainties ( $k = 2$ )	reported uncertainties included installation effects ( $k = 2$ )	reported uncertainties ( $k = 1$ ) with stability uncertainty			degree of equivalence	normalized difference	by Nielsen	by Cox
Labor	$x_i$	$d_i$	$U(x_i)$	$U(x_i)$	$u(x_i)$	$x_i/u^2(x_i)$	$1/u^2(x_i)$	$d_i$	norm $d_i$	$\chi^2$	$\chi^2$
Austria	-0,13	0,04	0,03	0,07	0,034	-116	889	-0,04	1,16	1,35	1,12
Slovakia	-0,03	0,06	0,11	0,13	0,063	-8	255	0,06	1,06	1,12	1,06
Czech Rep.	-0,01	0,08	0,12	0,13	0,067	-2	222	0,08	1,29	1,66	1,59
Switzerland	-0,04	0,05	0,18	0,19	0,095	-4	111	0,05	0,58	0,34	0,33
Sweden	-0,07	0,02	0,08	0,10	0,050	-28	400	0,02	0,51	0,26	0,24
Denmark	-0,05	0,04	0,11	0,13	0,063	-13	255	0,04	0,73	0,53	0,50
Germany	-0,05	0,04	0,03	0,07	0,034	-44	889	0,04	1,46	2,13	1,76
Slovenia	-0,13	0,04	0,17	0,18	0,090	-16	123	-0,04	0,40	0,16	0,15
France	0,00	0,09	0,12	0,13	0,067	0	222	0,09	1,44	2,07	1,99
Norway	-0,29	0,35	0,08	0,10	0,050	-116	400	-0,20	4,07	16,57	15,28
Turkey	-0,13	0,04	0,05	0,08	0,038	-92	711	-0,04	1,02	1,04	0,90
Hungary	-0,01	0,08	0,11	0,13	0,063	-3	255	0,08	1,38	1,91	1,82
Lithuania	-0,16	0,07	0,14	0,15	0,076	-28	172	-0,07	0,87	0,76	0,74
Italy	-0,07	0,02	0,11	0,13	0,064	-17	248	0,02	0,40	0,16	0,15
mean = $x_{ref}$	-0,084				Summen =	-487				$\chi^2_{obs} =$	$\chi^2_{obs} =$
s	0,079				Summen =		5152			30,07	27,63
$s_0$	0,026									0,46%	1,02%
$\nu =$	13									$P\{\chi^2(\nu) > \chi^2_{obs}\} =$	
$x_{ref} =$	-0,095									level of significance = 5 %	
						$u^2(x_{ref}) = 1,941E-04$	% <sup>2</sup>				
						$u(x_{ref}) = 0,014$	%				

**Example: - 11 participants,  $\nu = 10$  (without Cz, F, N) 857 downstream**

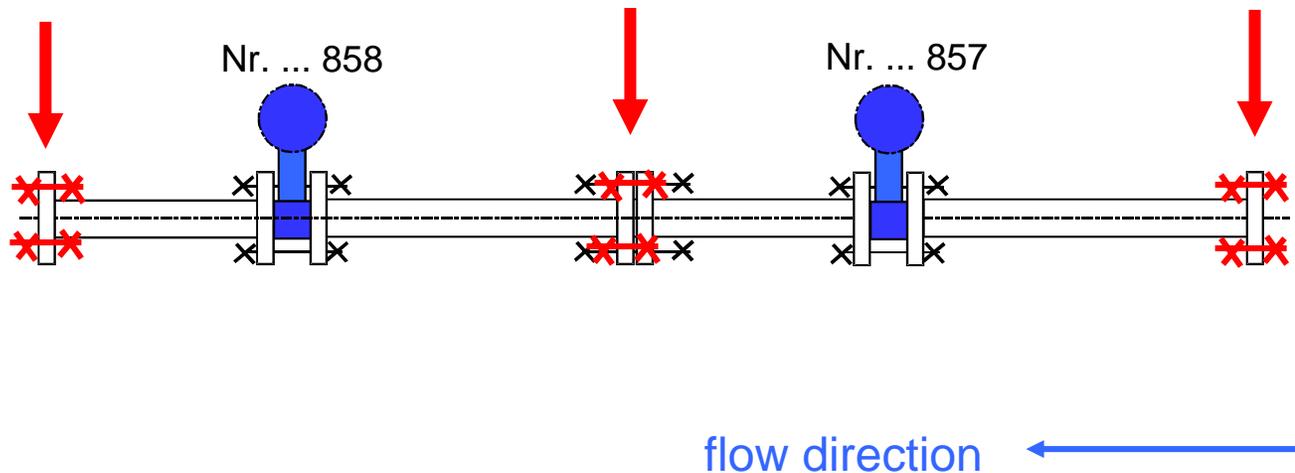
	reported values	abs deviation from mean	reported uncertainties ( $k = 2$ )	reported uncertainties included installation effects ( $k = 2$ )	reported uncertainties ( $k = 1$ ) with stability uncertainty			degree of equivalence	normalized difference	by Nielsen	by Cox
Labor	$x_i$	$d_i$	$U(x_i)$	$U(x_i)$	$u(x_i)$	$x_i/u^2(x_i)$	$1/u^2(x_i)$	$d_i$	norm $d_i$	$\chi^2$	$\chi^2$
Austria	-0,13	0,04	0,03	0,07	0,034	-116	889	-0,04	1,49	2,21	1,75
Slovakia	-0,03	0,06	0,11	0,13	0,063	-8	255	0,06	0,92	0,84	0,79
Switzerland	-0,04	0,05	0,18	0,19	0,095	-4	111	0,05	0,49	0,24	0,23
Sweden	-0,07	0,02	0,08	0,10	0,050	-28	400	0,02	0,33	0,11	0,10
Denmark	-0,05	0,04	0,11	0,13	0,063	-13	255	0,04	0,59	0,34	0,32
Germany	-0,05	0,04	0,03	0,07	0,034	-44	889	0,04	1,19	1,42	1,13
Slovenia	-0,13	0,04	0,17	0,18	0,090	-16	123	-0,04	0,50	0,25	0,24
Turkey	-0,13	0,04	0,05	0,08	0,038	-92	711	-0,04	1,30	1,68	1,40
Hungary	-0,01	0,08	0,11	0,13	0,063	-3	255	0,08	1,24	1,55	1,46
Lithuania	-0,16	0,07	0,14	0,15	0,076	-28	172	-0,07	1,00	0,99	0,95
Italy	-0,07	0,02	0,11	0,13	0,064	-17	248	0,02	0,25	0,06	0,06
<b>mean = <math>x_{ref}</math></b>	<b>-0,079</b>				Summen =	<b>-369</b>				$\chi^2_{obs} =$	$\chi^2_{obs} =$
<b>s</b>	<b>0,050</b>				Summen =		<b>4308</b>			<b>9,69</b>	<b>8,43</b>
<b><math>s_0</math></b>	<b>0,017</b>									<b>46,84%</b>	<b>58,66%</b>
<b><math>\nu =</math></b>	<b>10</b>									<b>level of significance = 5%</b>	
<b><math>x_{ref} =</math></b>	<b>-0,086</b>										
						<b><math>u^2(x_{ref}) = 2,221E-04</math></b>		% <sup>2</sup>			
						<b><math>u(x_{ref}) = 0,015</math></b>		%			

## Stability of the meters

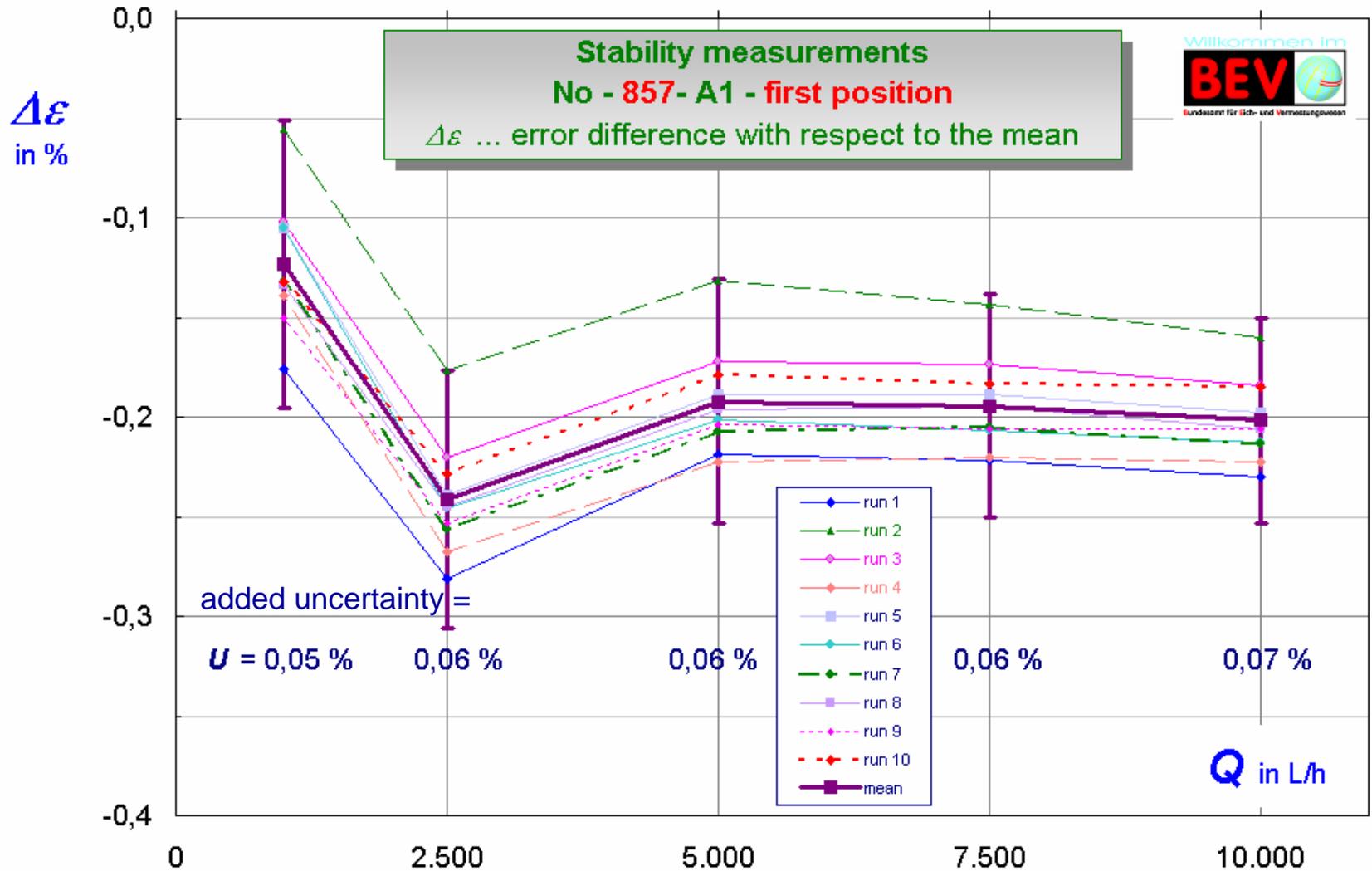
We observed that the meters depend from **installation conditions!**

Experiment: We detach the screws shown in the following picture  
After that we fasten the screws again. **We do this 10 times.**

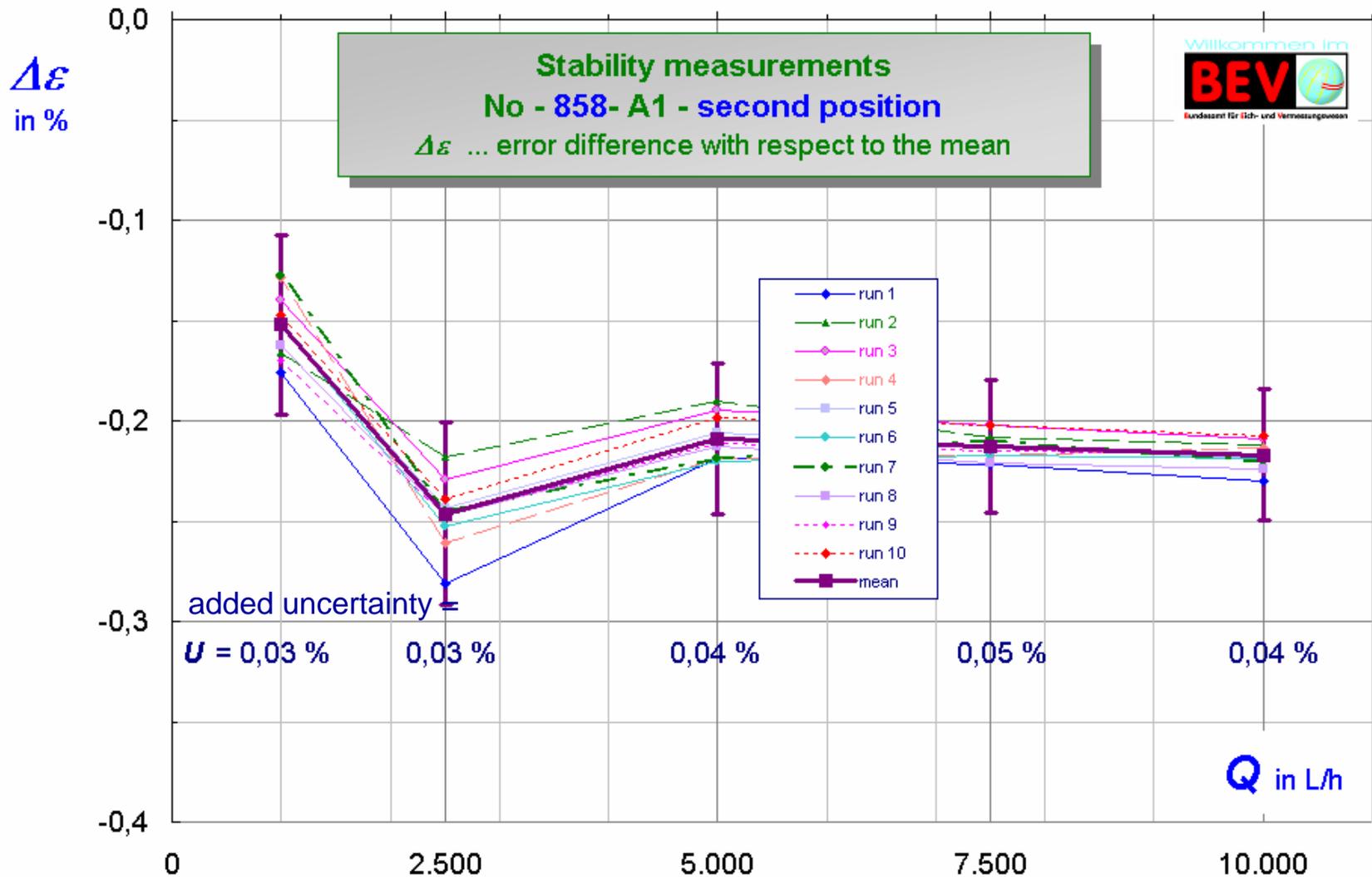
What do we get?



# meter 857 at first position (upstream)



**meter 857 at second position (downstream)**



## Uncertainty test rig and meters

## Uncertainty of installation

### Summary:

- first position (upstream): +/- 0,6 %
  
- second position (downstream): +/- 0,3 %

**!! We use that as a part of uncertainty which is regarded in the following Youden plots !!**

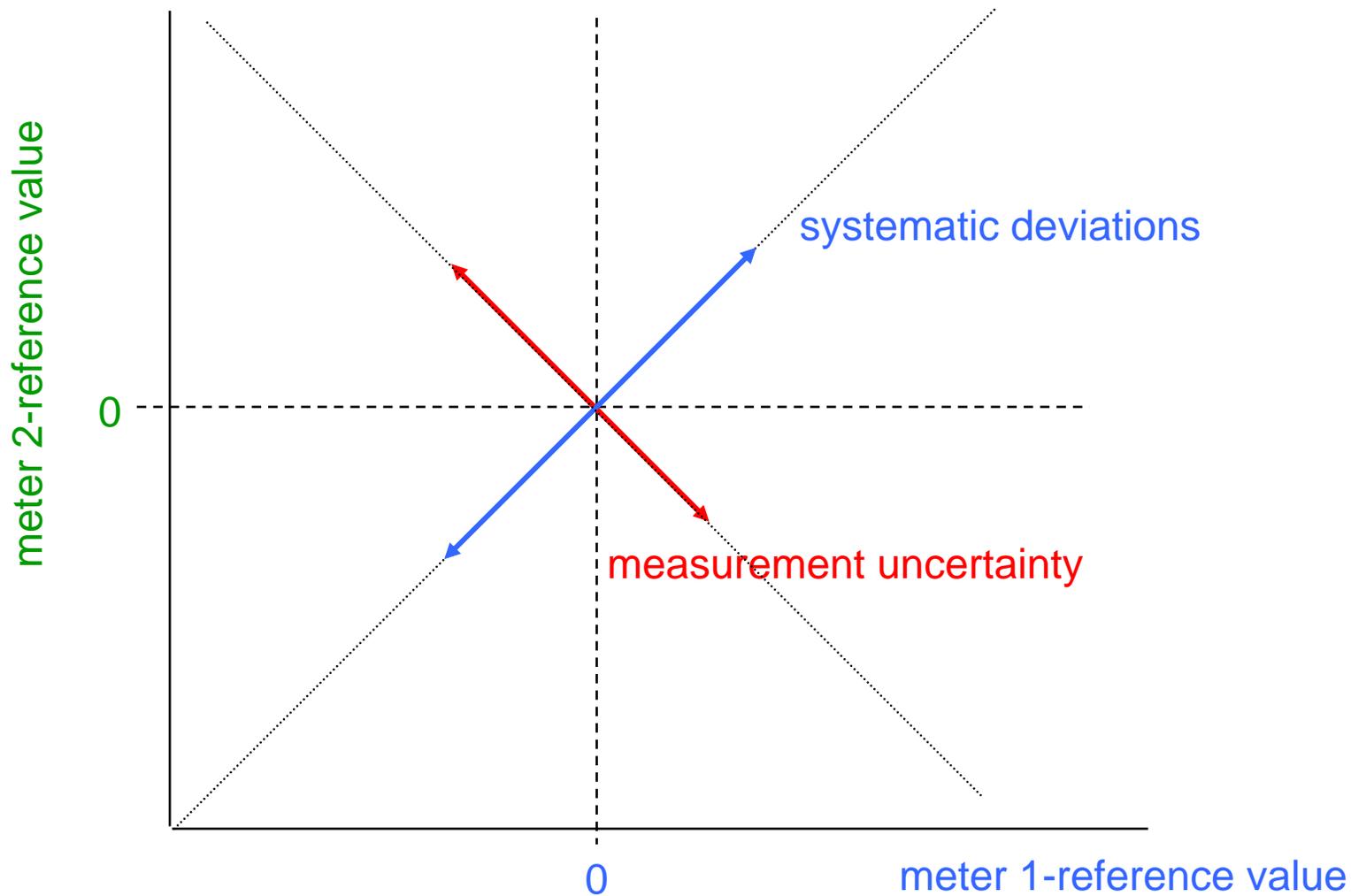
# Youden-plots

## The concept of „Youden plot“

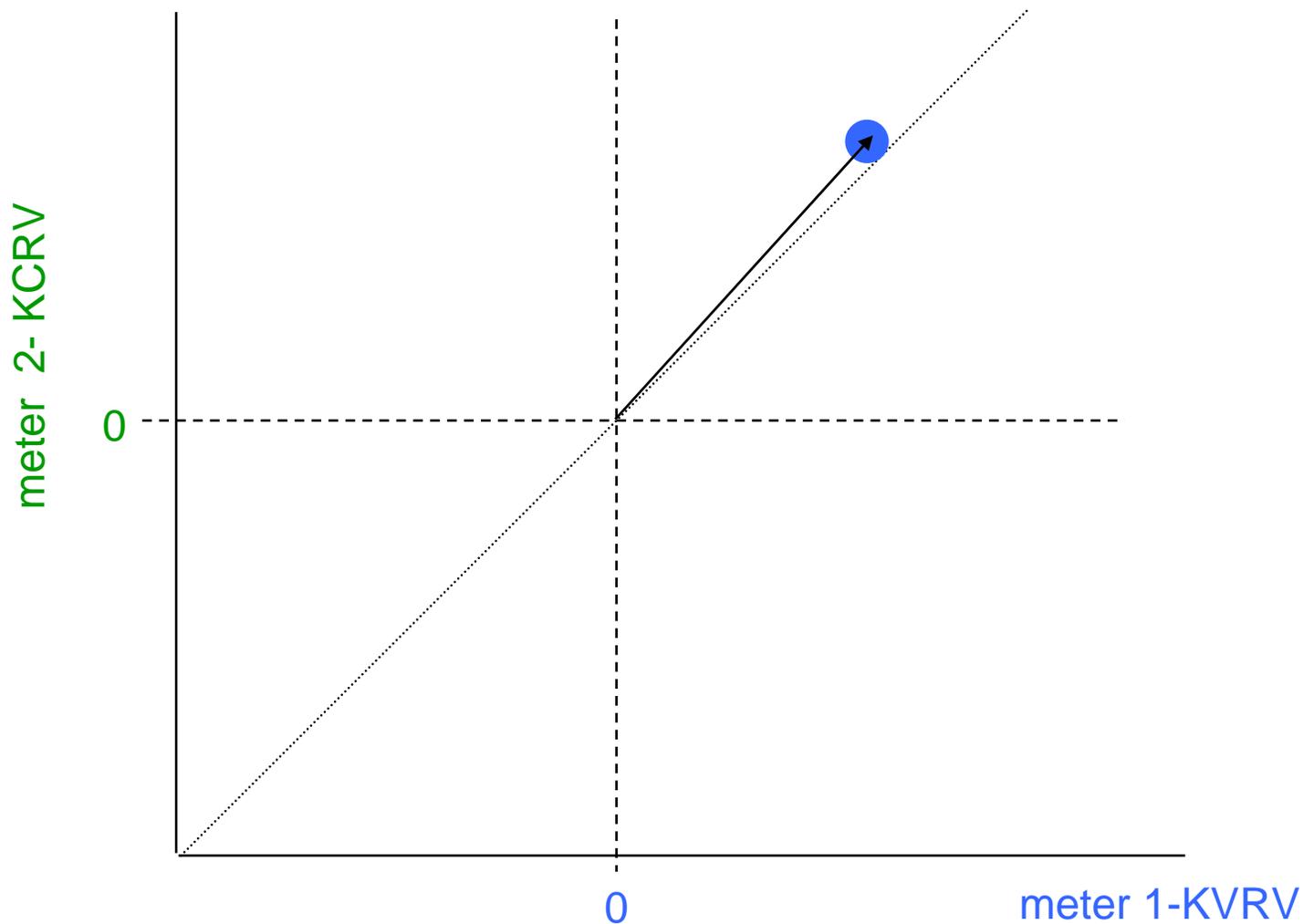
### PLEASE REMEMBER:

- On the x-axis there is the difference between the measurement value and the KCRV for the first meter, on the y-axis there is the same for the second meter
- Zero is on both axis the **KCRV**

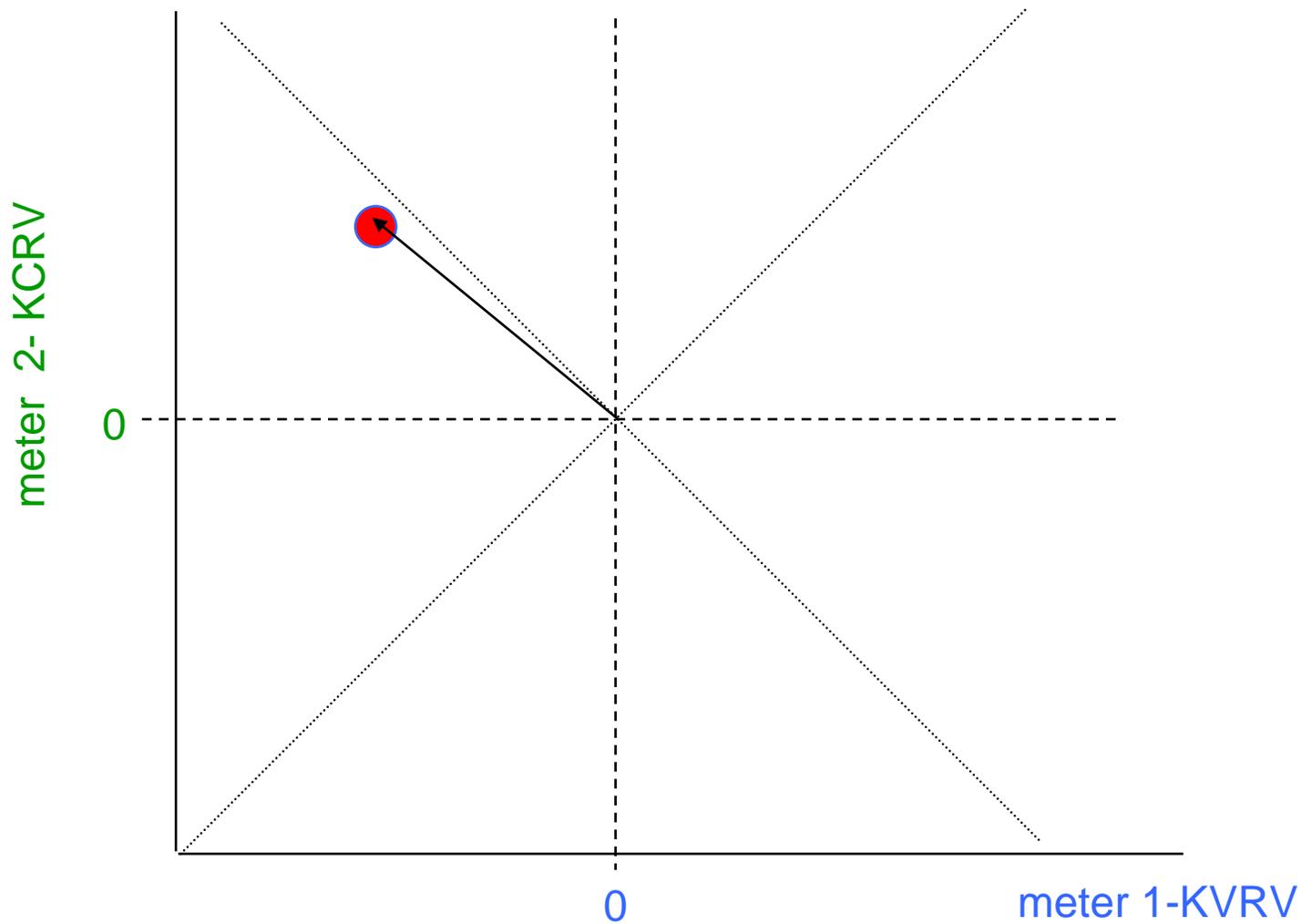
## The sense of Youden-plot



**typical: small uncertainty, large systematic error**



**typical: large uncertainty, small systematic error**

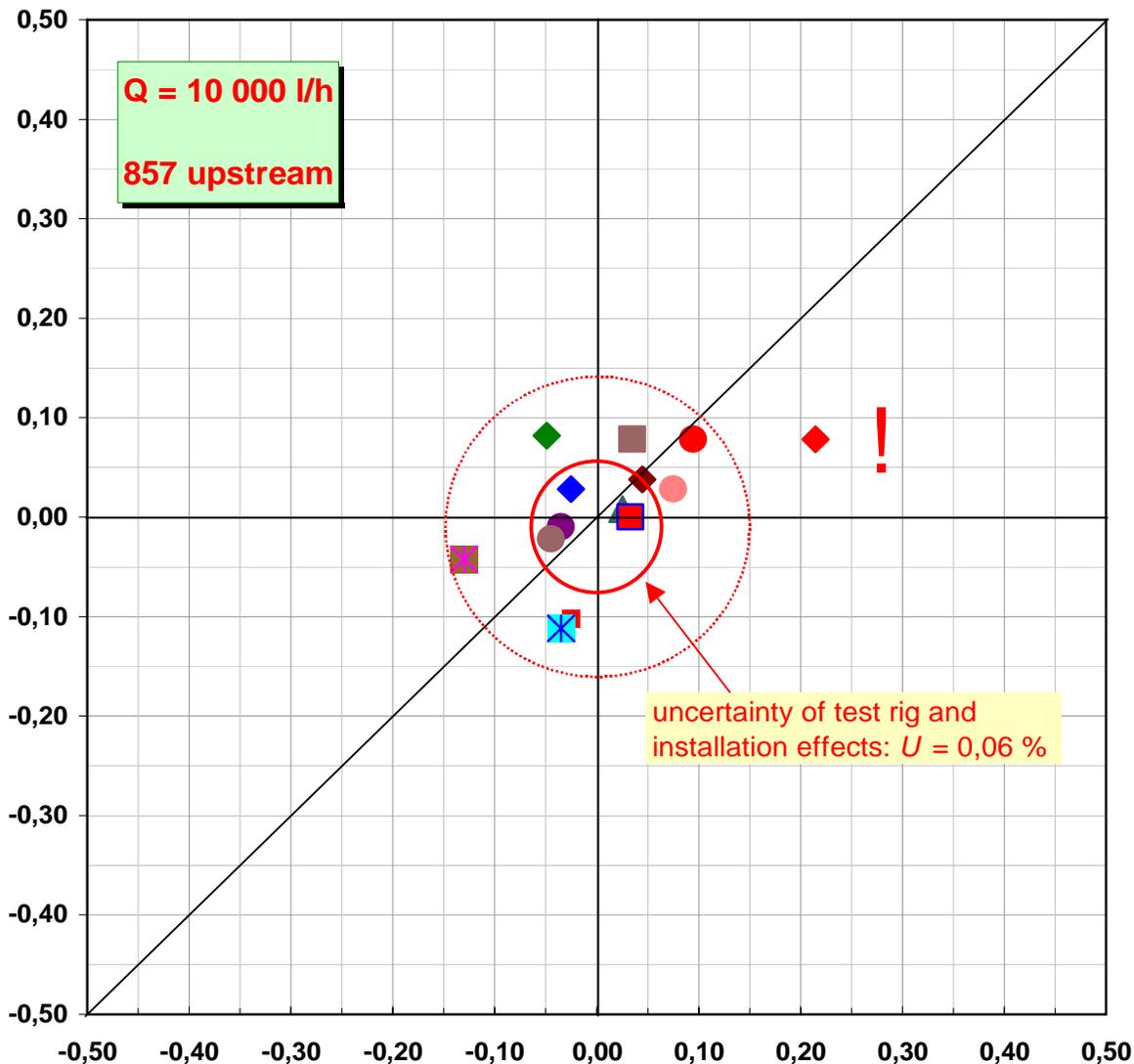


# Results of the EUROMET comparisons

reference: KCRV (method → Lau, 2003)

**Q = 10 000 L/h, 857 upstream**

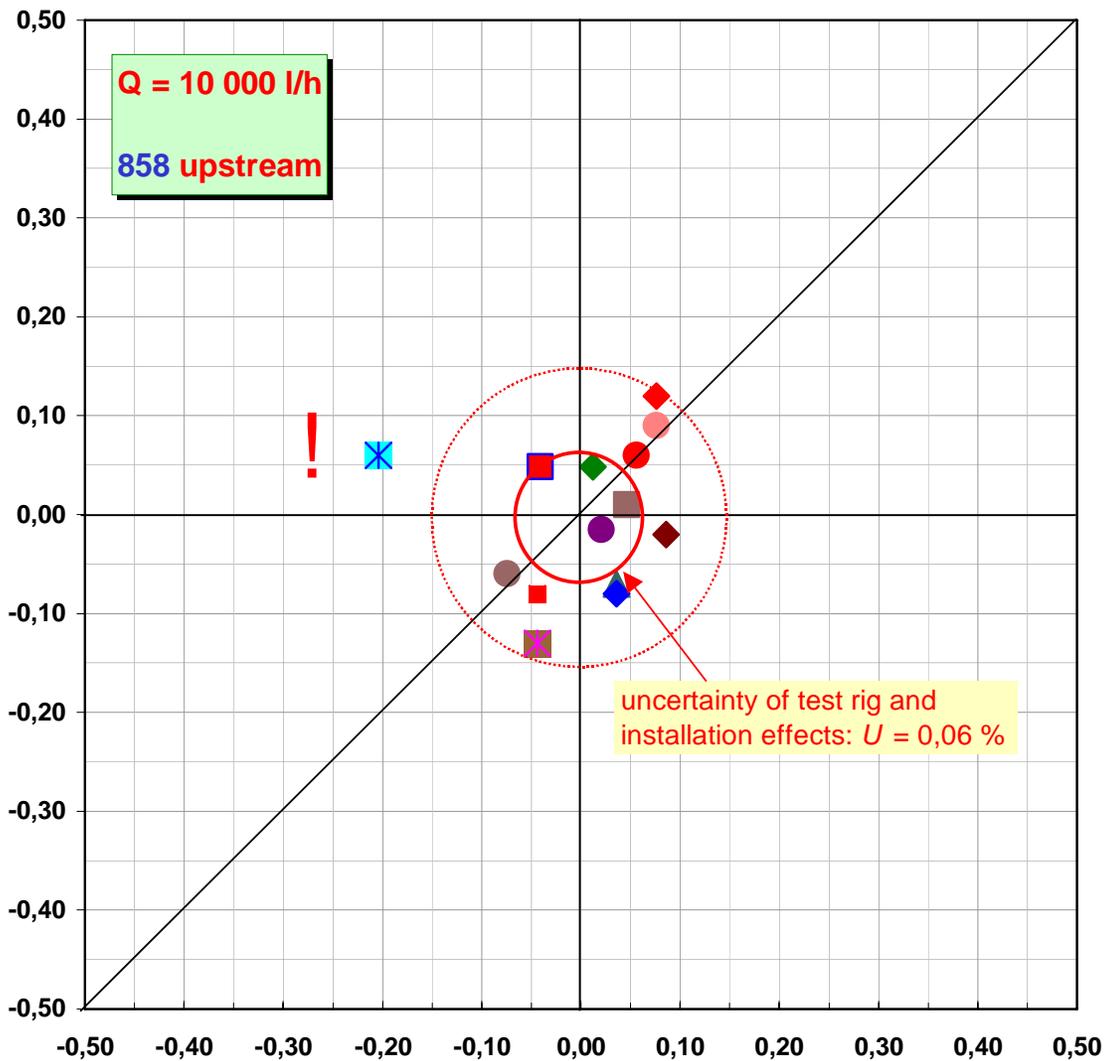
$F_{A2,858}$



$F_{A1,857}$

**Q = 10 000 L/h, 858 upstream**

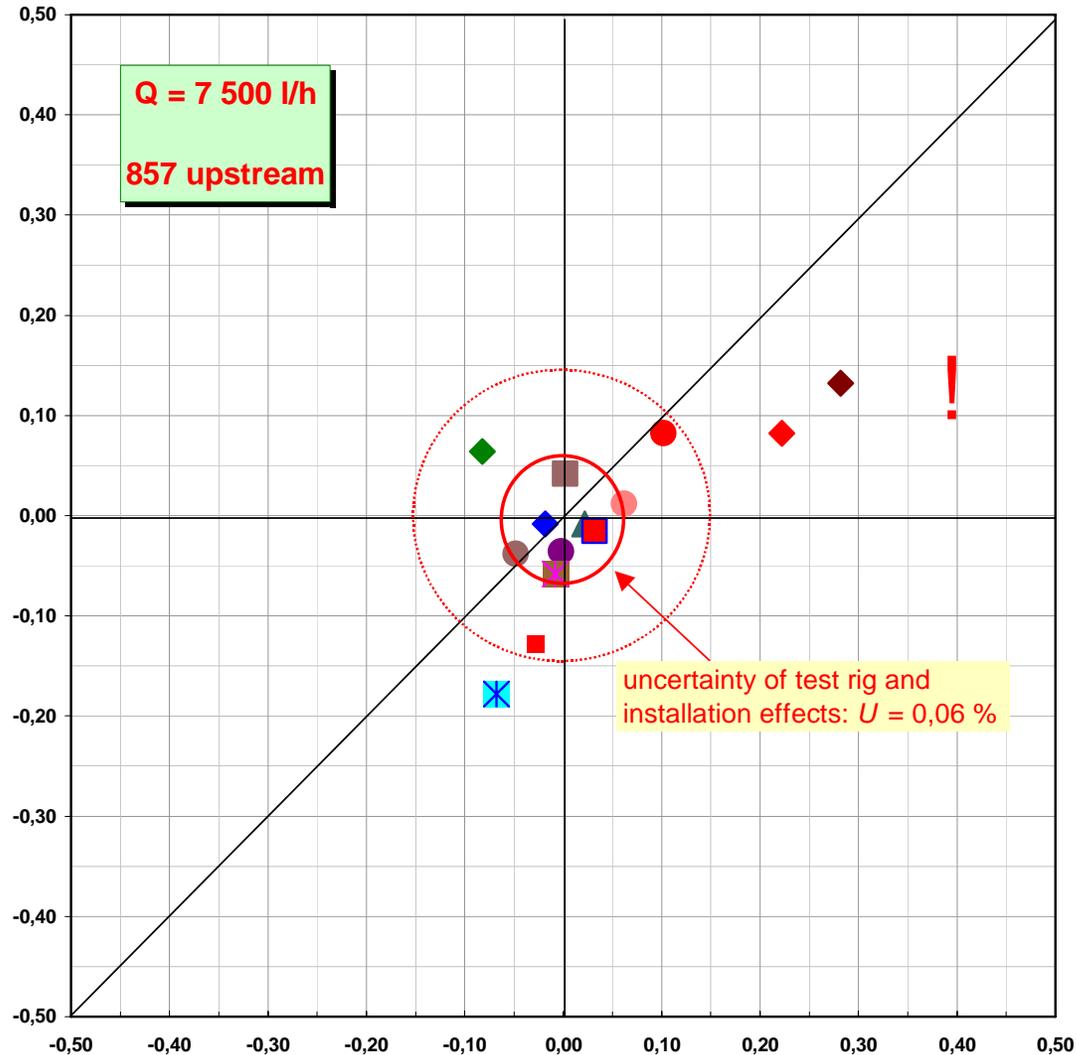
$F_{A1,858}$



$F_{A2,857}$

**Q = 7 500 L/h, 857 upstream**

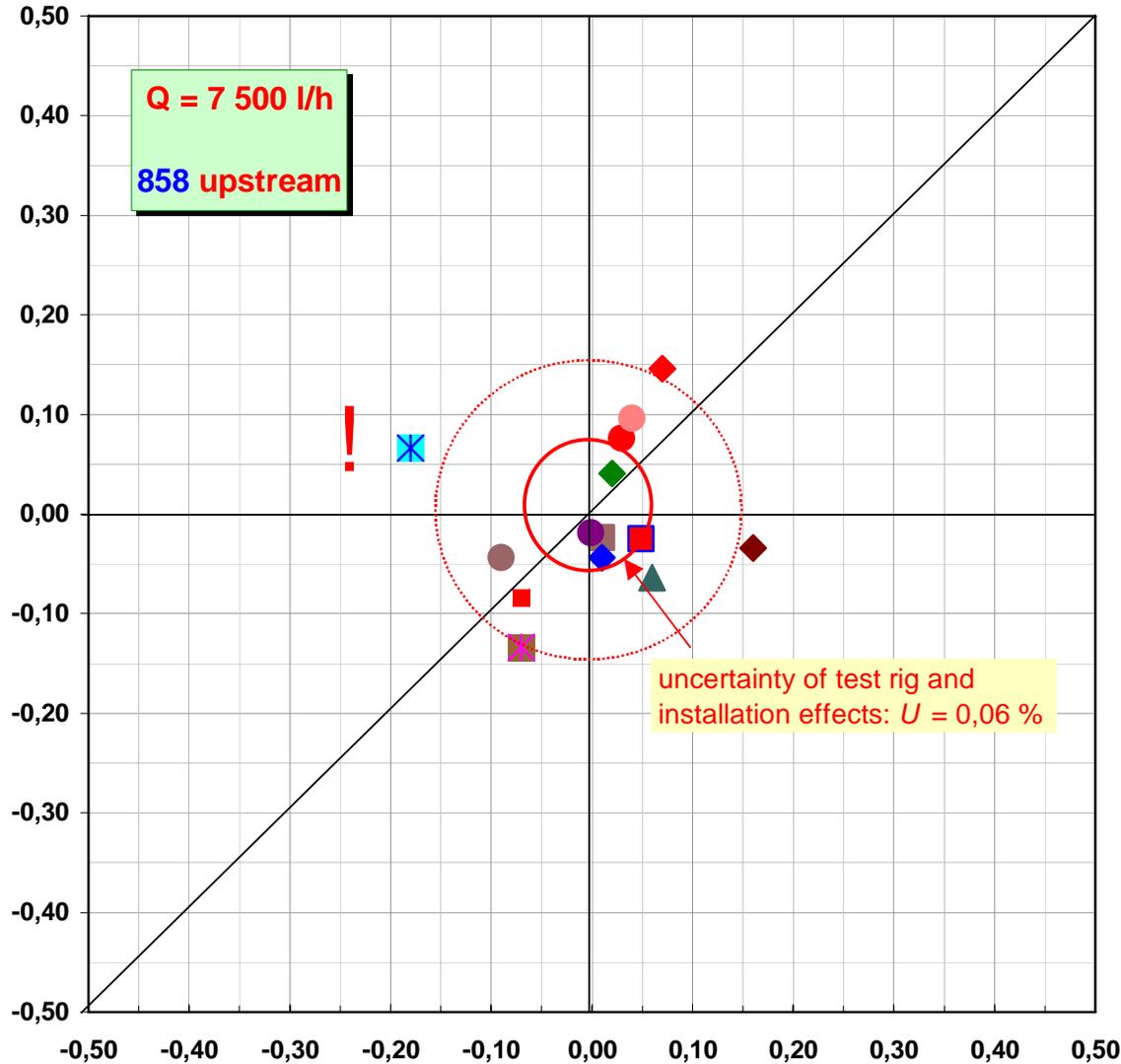
$F_{A2,858}$



$F_{A1,857}$

**Q = 7 500 L/h, 858 upstream**

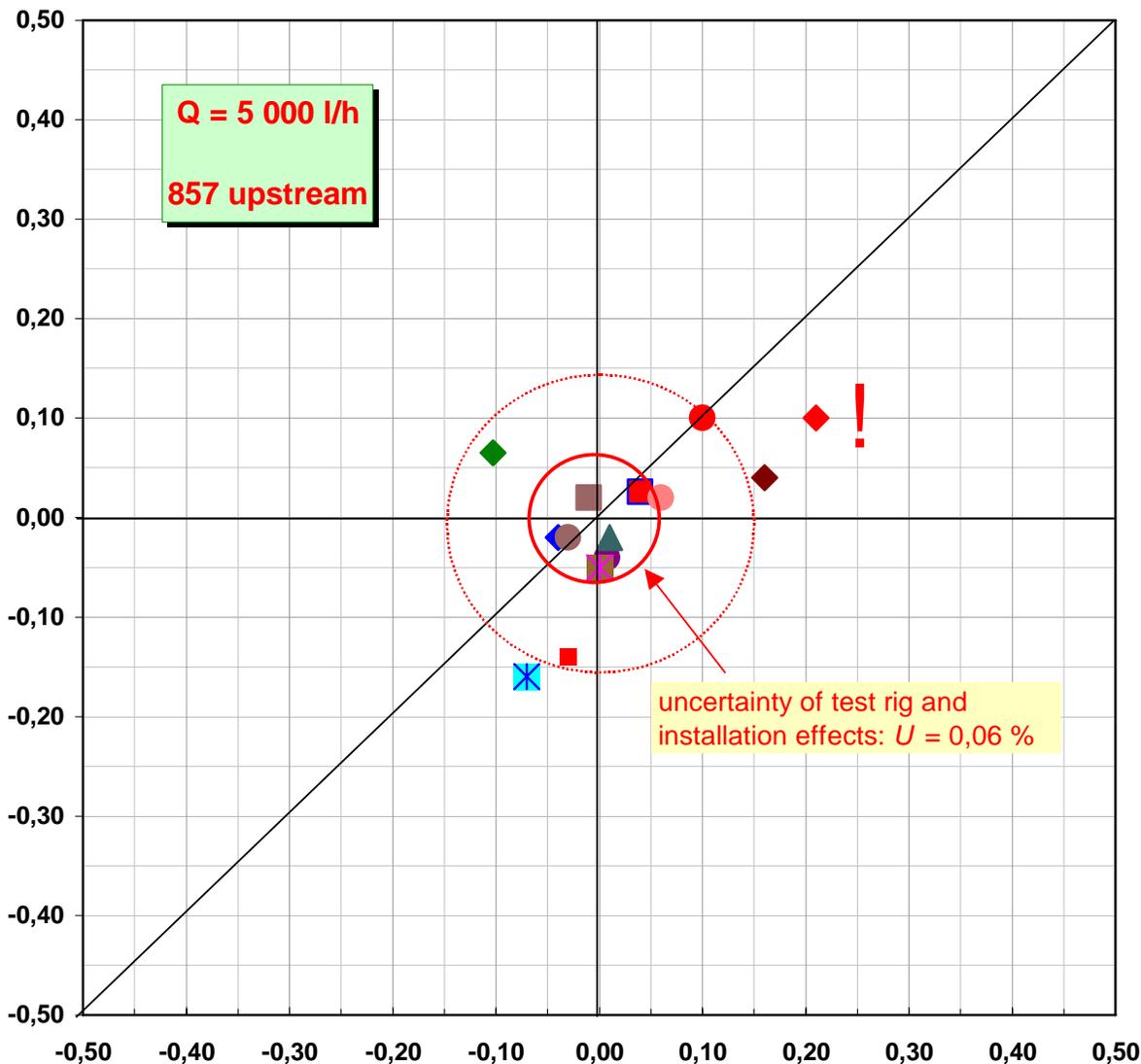
$F_{A1,858}$



$F_{A2,857}$

**Q = 5 000 L/h, 857 upstream**

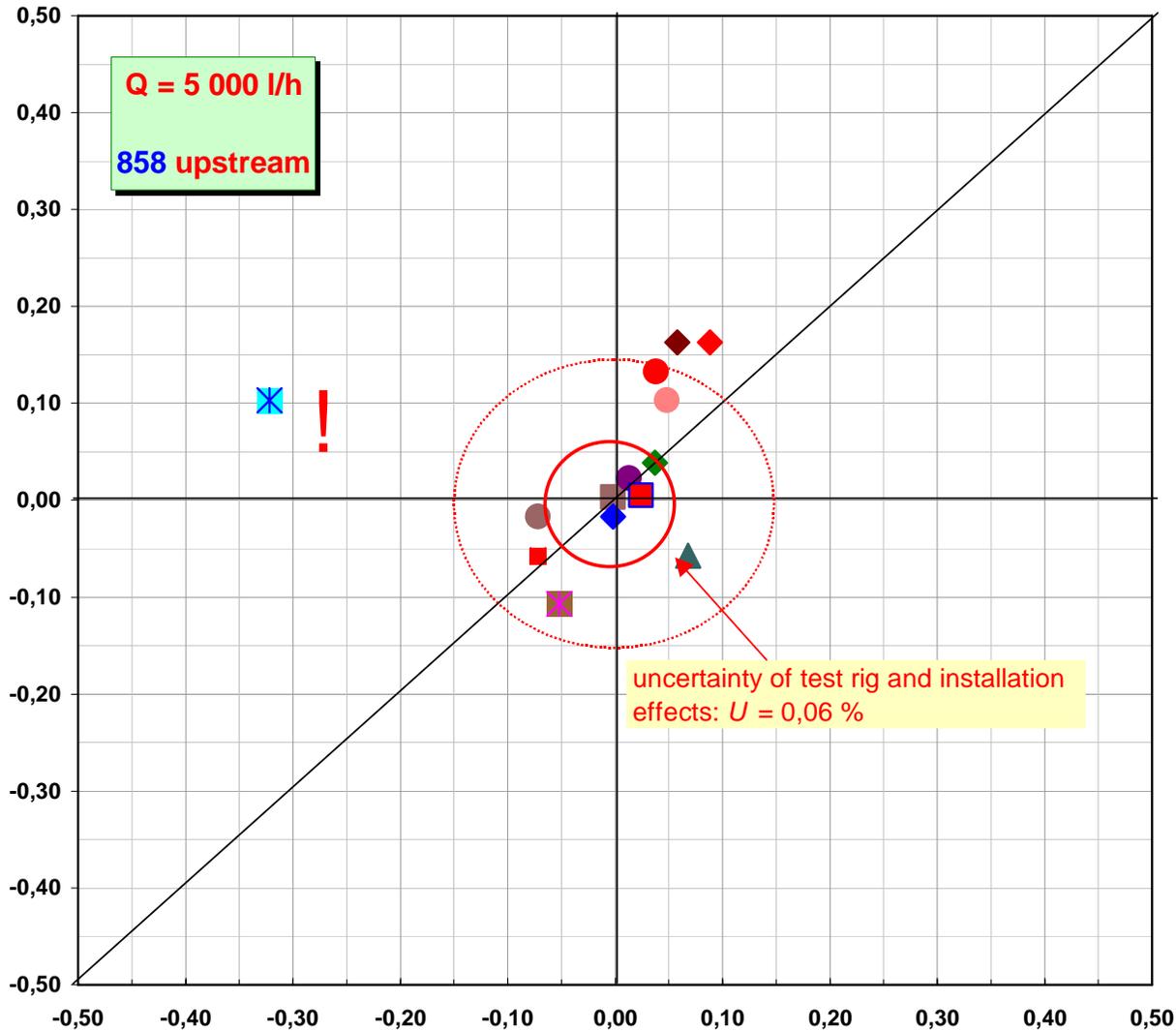
$F_{A2,858}$



$F_{A1,857}$

**Q = 5 000 L/h, 858 upstream**

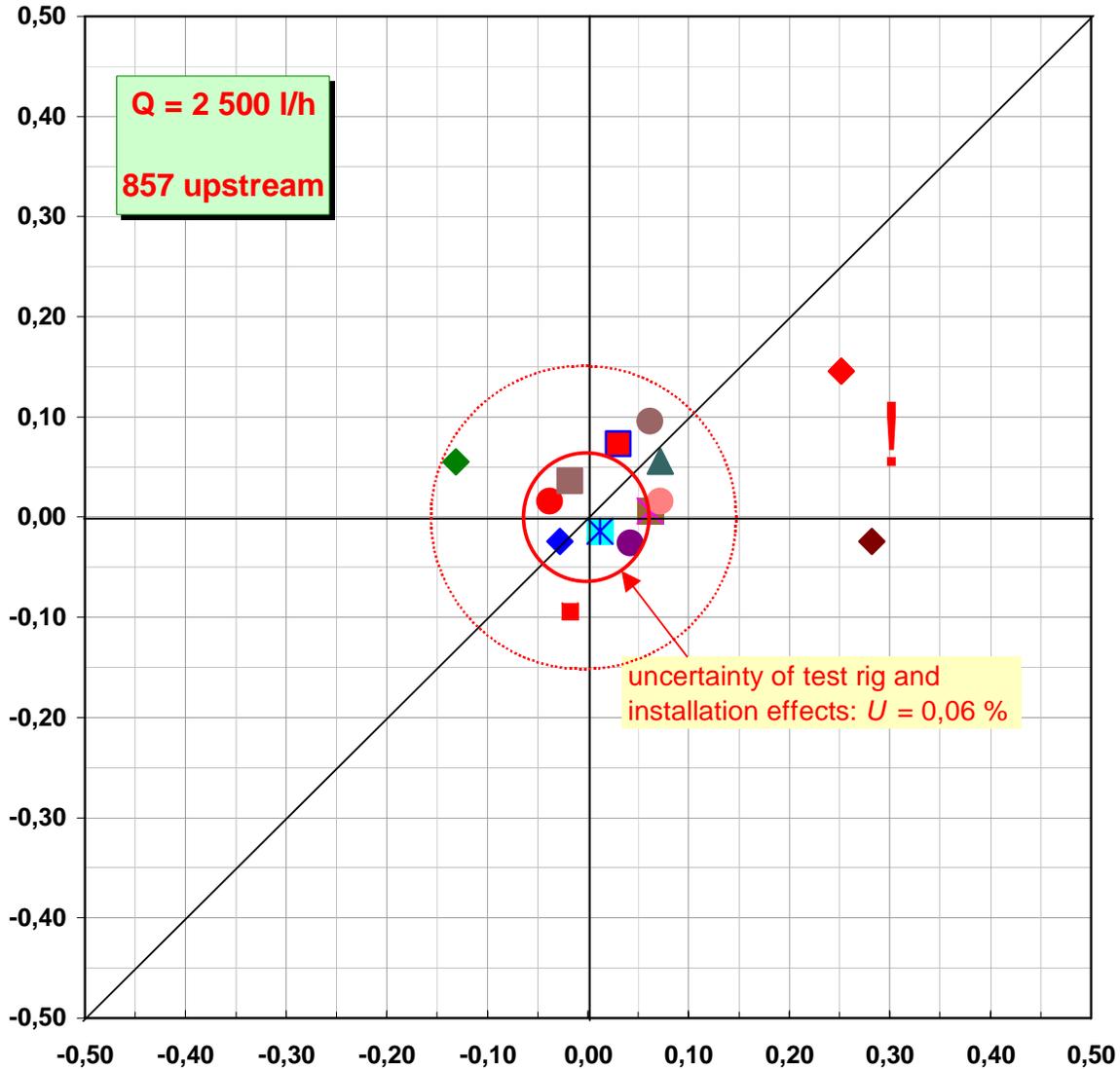
$F_{A1,858}$



$F_{A2,857}$

**Q = 2 500 L/h, 857 upstream**

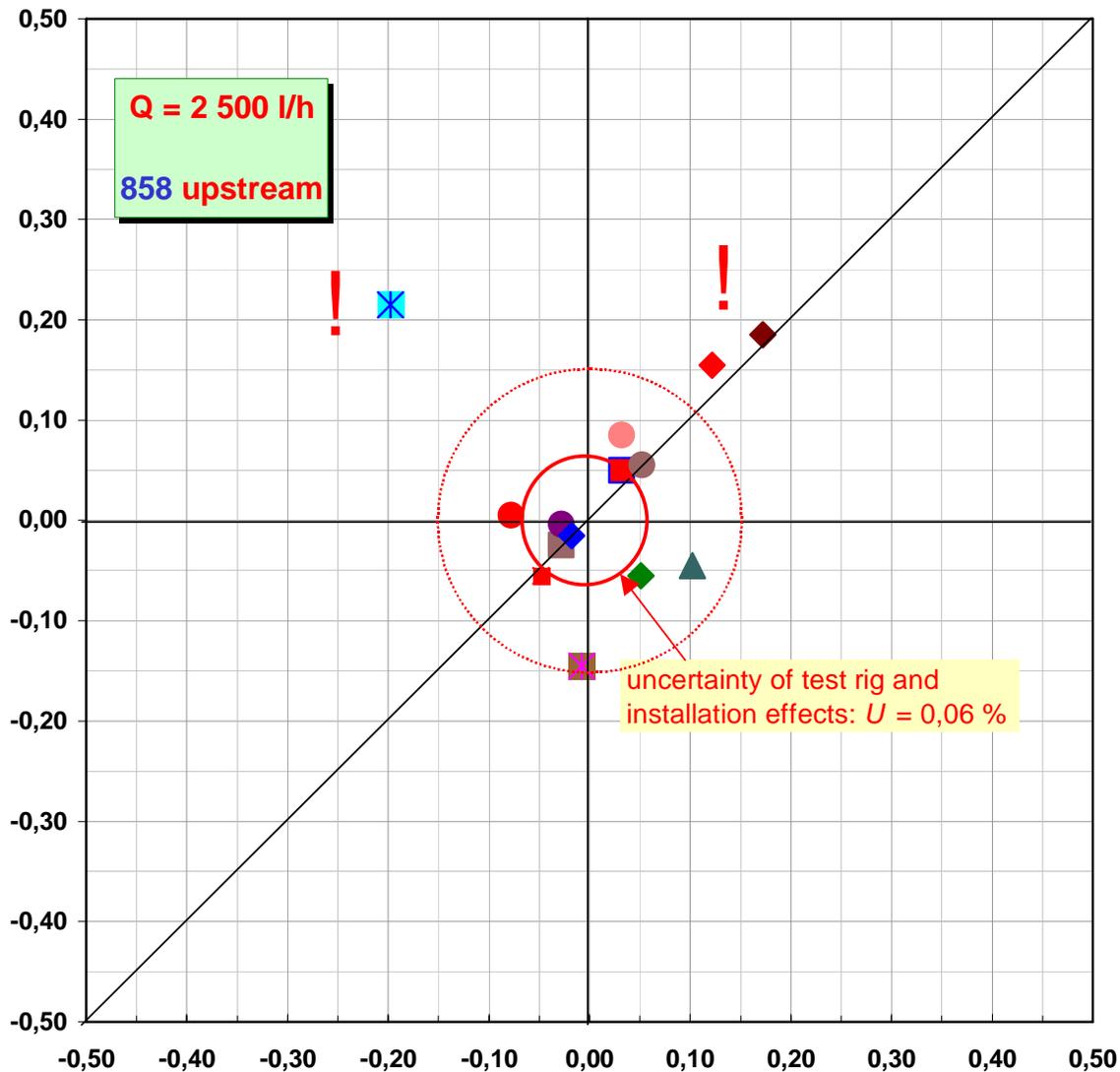
$F_{A2,858}$



$F_{A1,857}$

**Q = 2 500 L/h, 858 upstream**

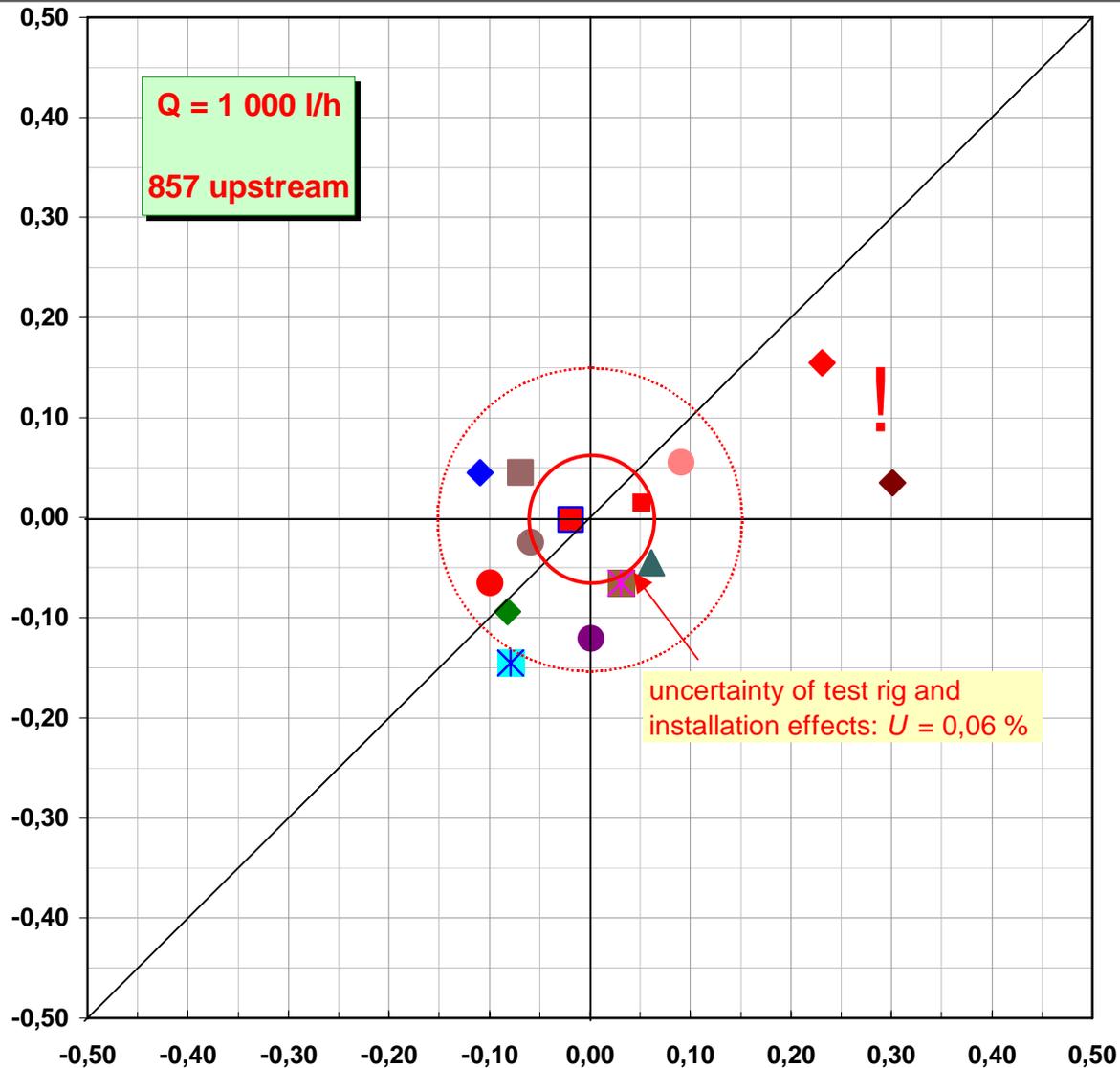
$F_{A1,858}$



$F_{A2,857}$

**Q = 1 000 L/h, 857 upstream**

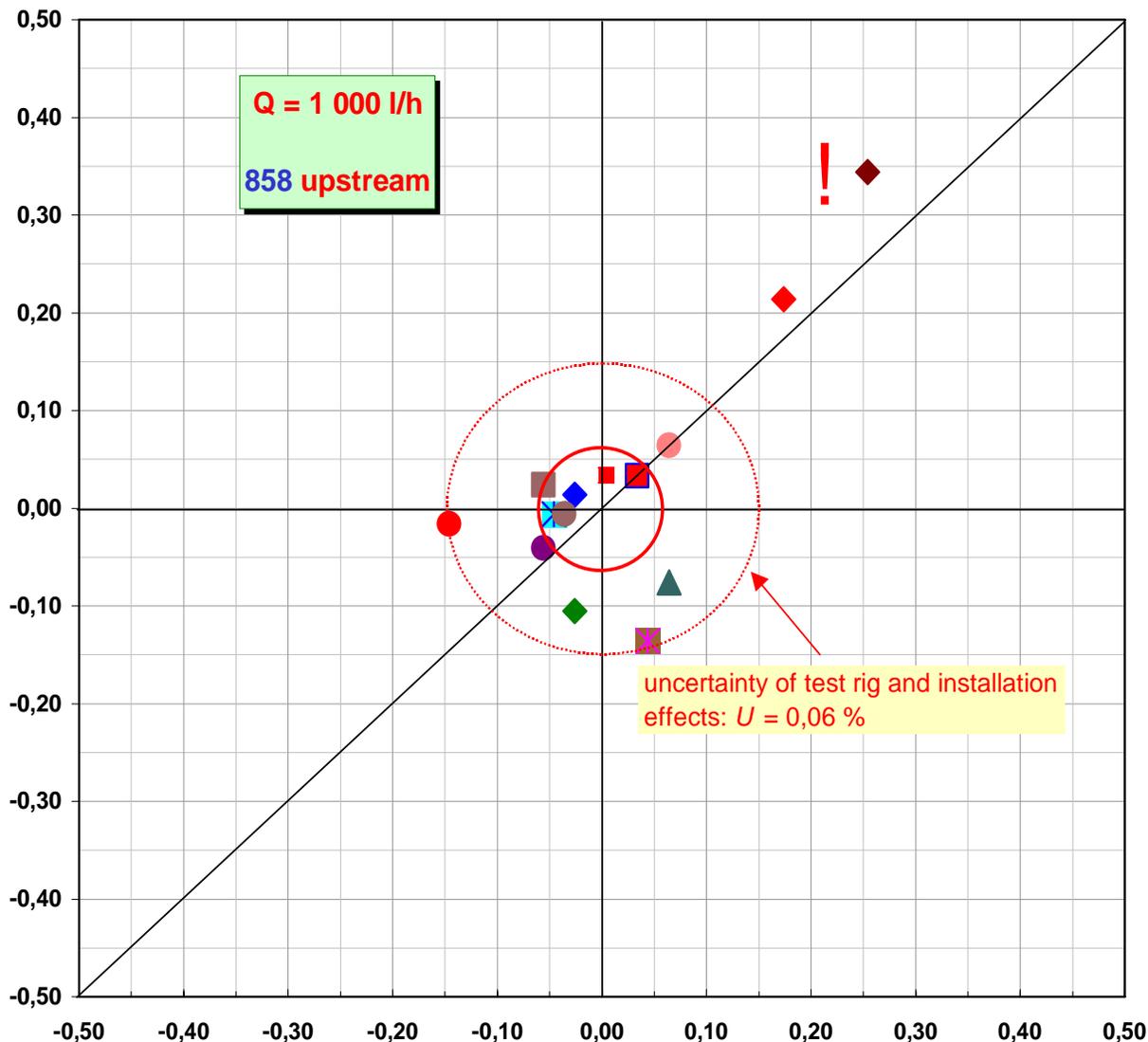
$F_{A2,858}$



$F_{A1,857}$

**Q = 1 000 L/h, 858 upstream**

$F_{A1,858}$



$F_{A2,857}$

## Are there some NMI's with systematic errors

What is to do: for determination of KCRV → elimination of the outsiders

→ criteria:  $P(\chi^2) > 5 \%$

## Results

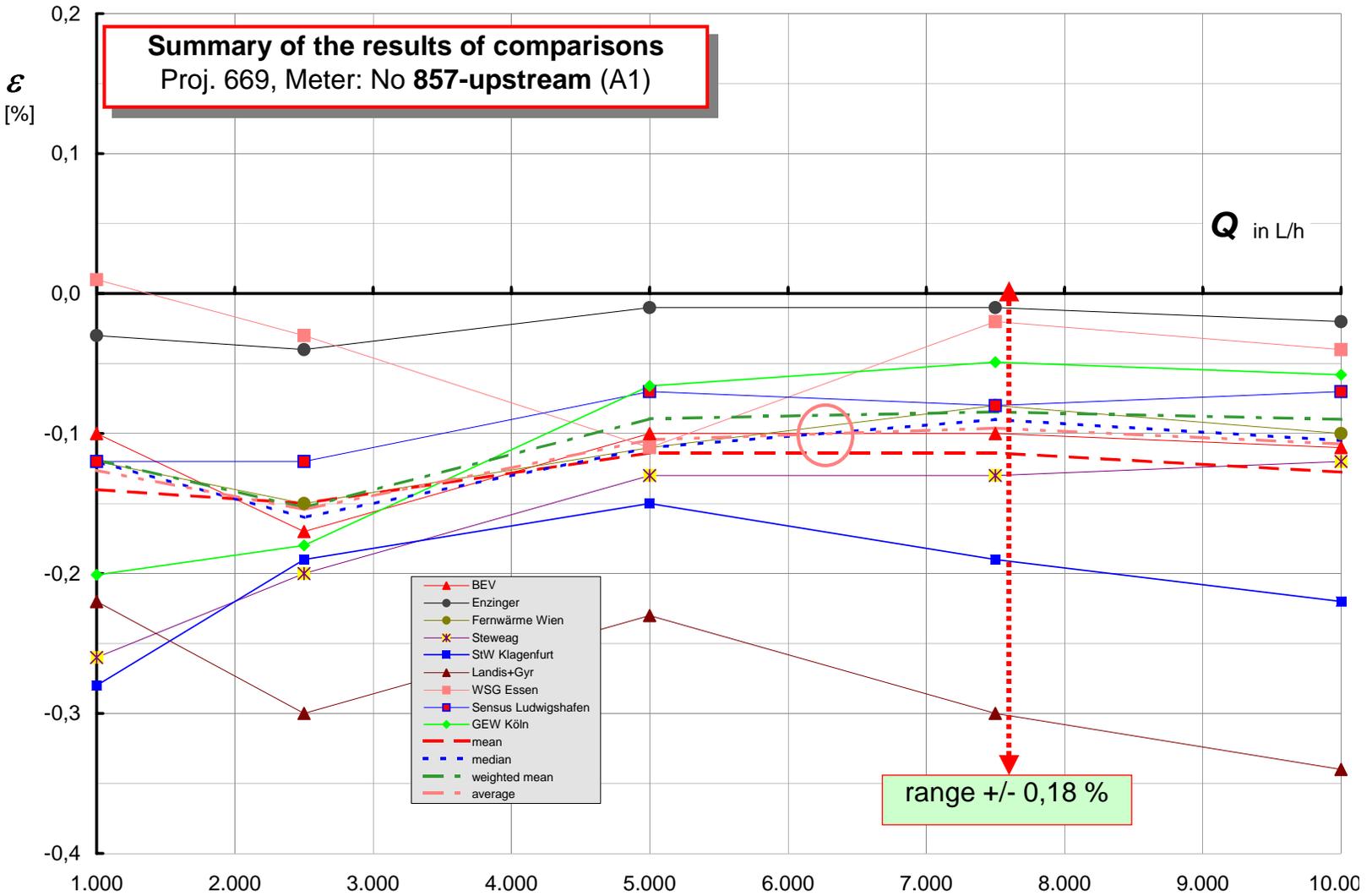
- measurement uncertainties of participants are extremely different: → (0,02 % bis 0,20 %)
- if measurement uncertainty of a NMI very small → the measurement results dominate the KCRV
- if measurement uncertainty of a NMI large → only a small contribution to KCRV evaluation
- please remember: installation effects are **not neglectable**

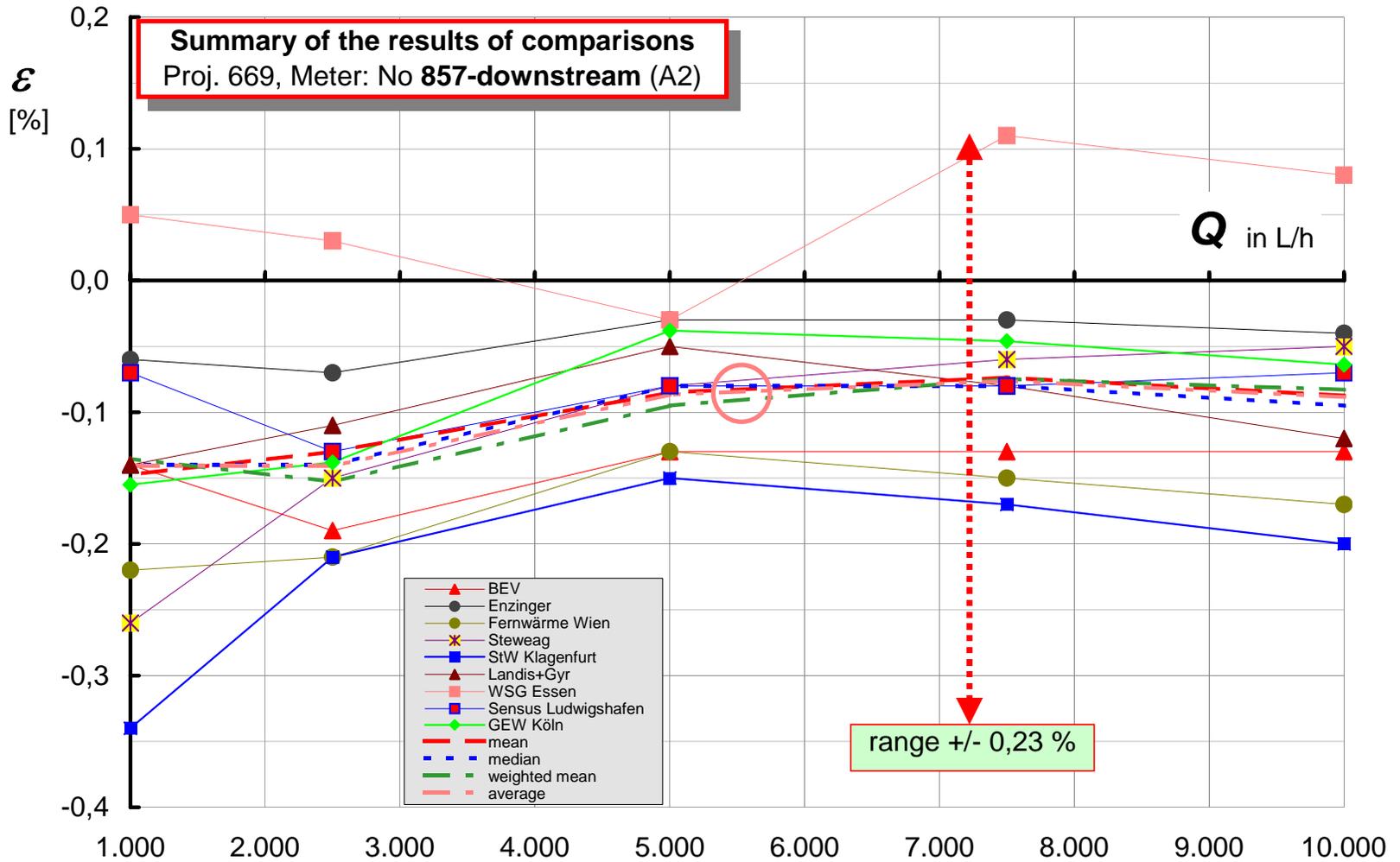
## Results of the measurements:

- ☀ 10 participant (77 %) lie in a range of  $\pm 0,15$  %
- ☀ 1 participant (7,6 %) lies in a range of  $\pm 0,25$  %
- ☀ 1 participant (7,6 %) lies in a range of  $\pm 0,30$  %
- ☀ 1 participant (7,6 %) lies in a range of  $\pm 0,32$  %

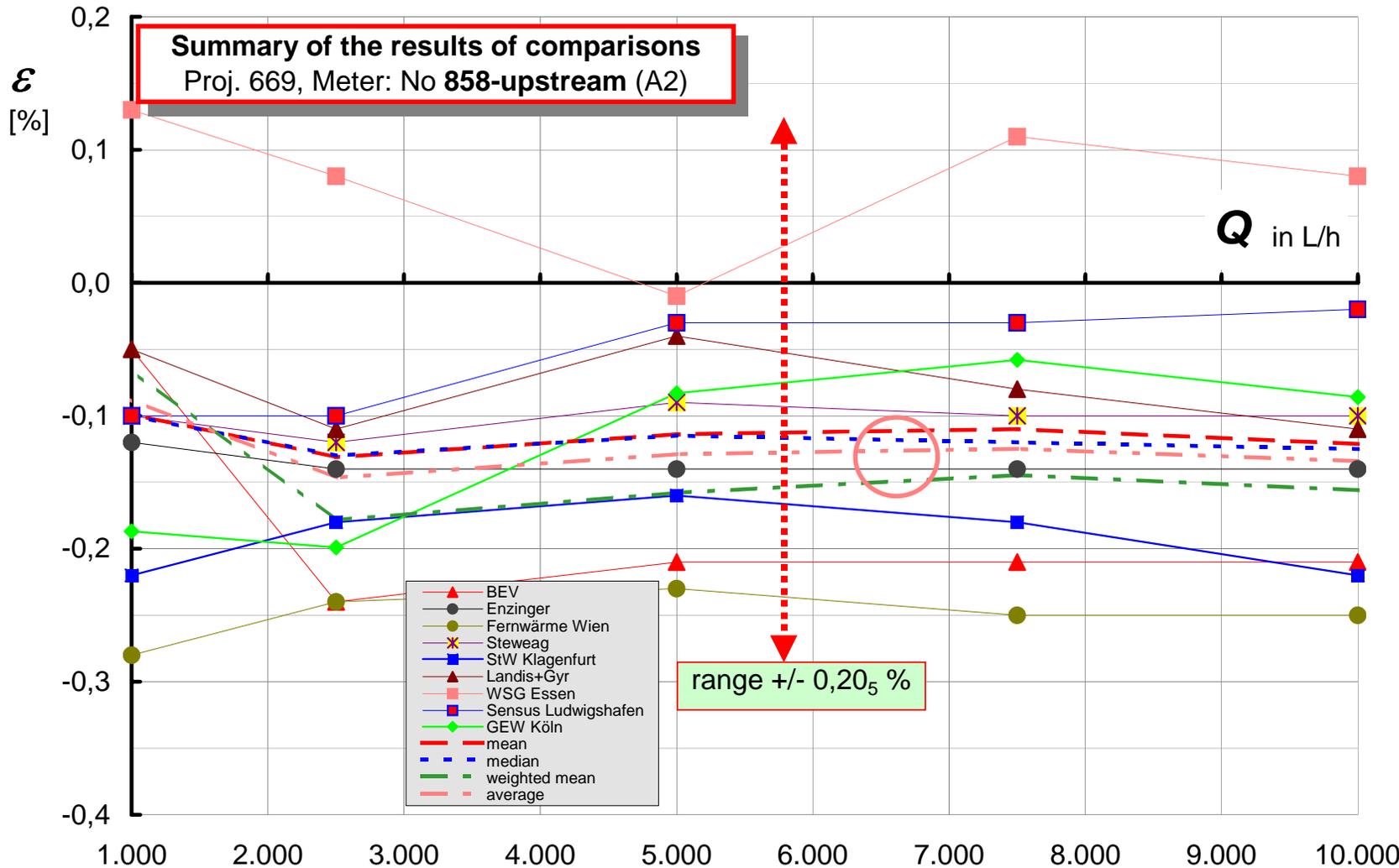
## Results in Verification offices

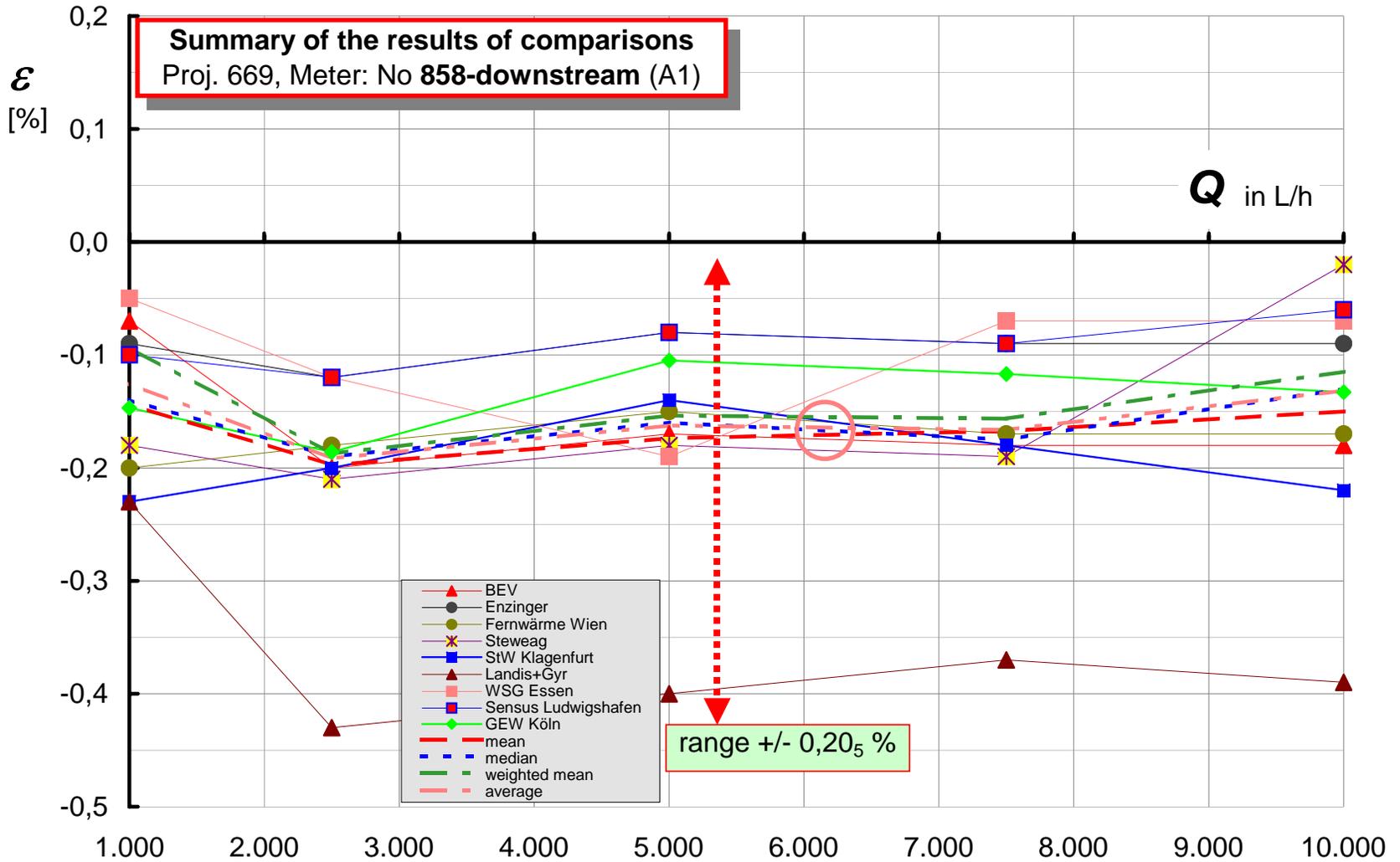
**No 857- upstream**





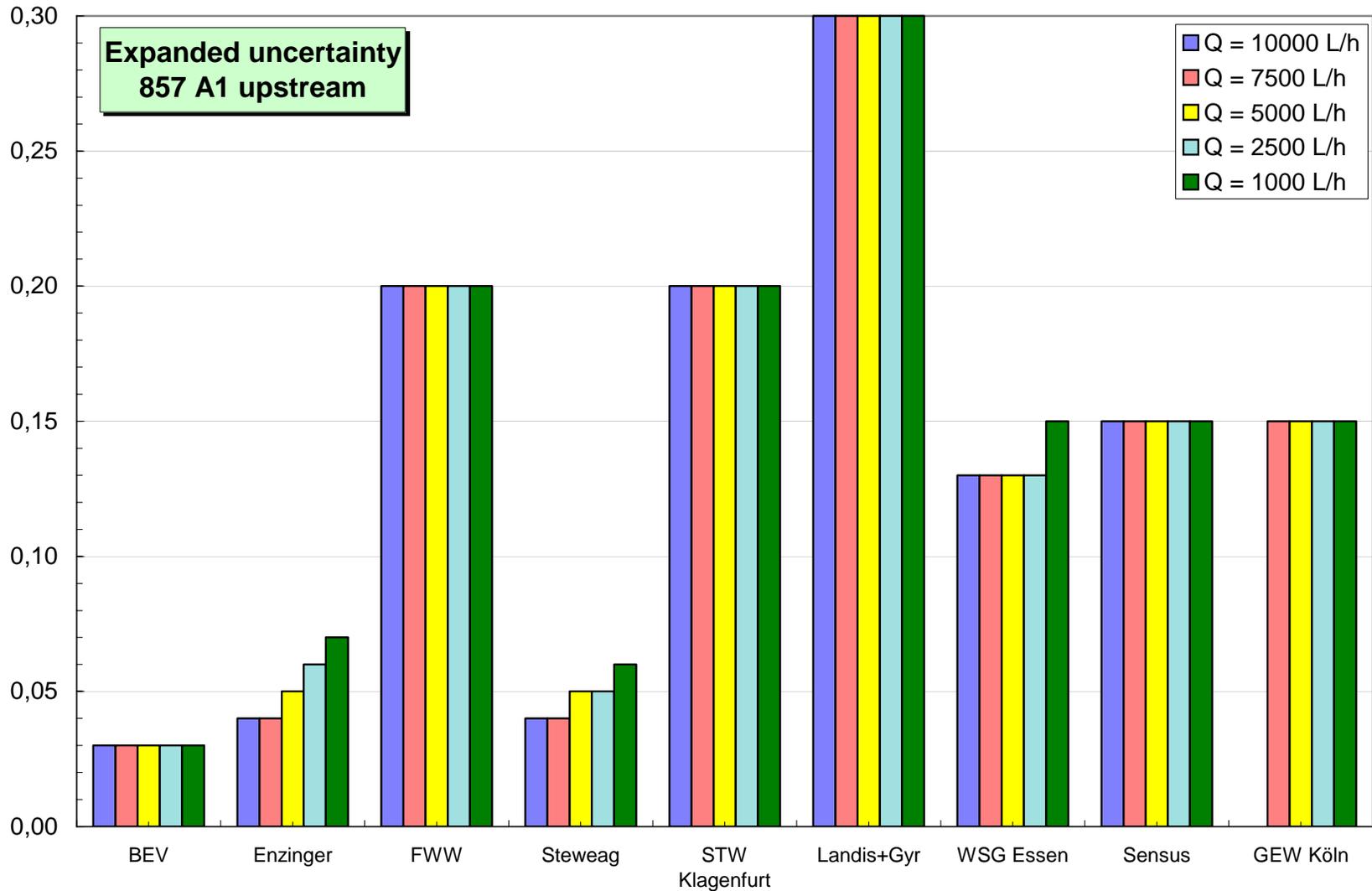
# No. 858 - upstream

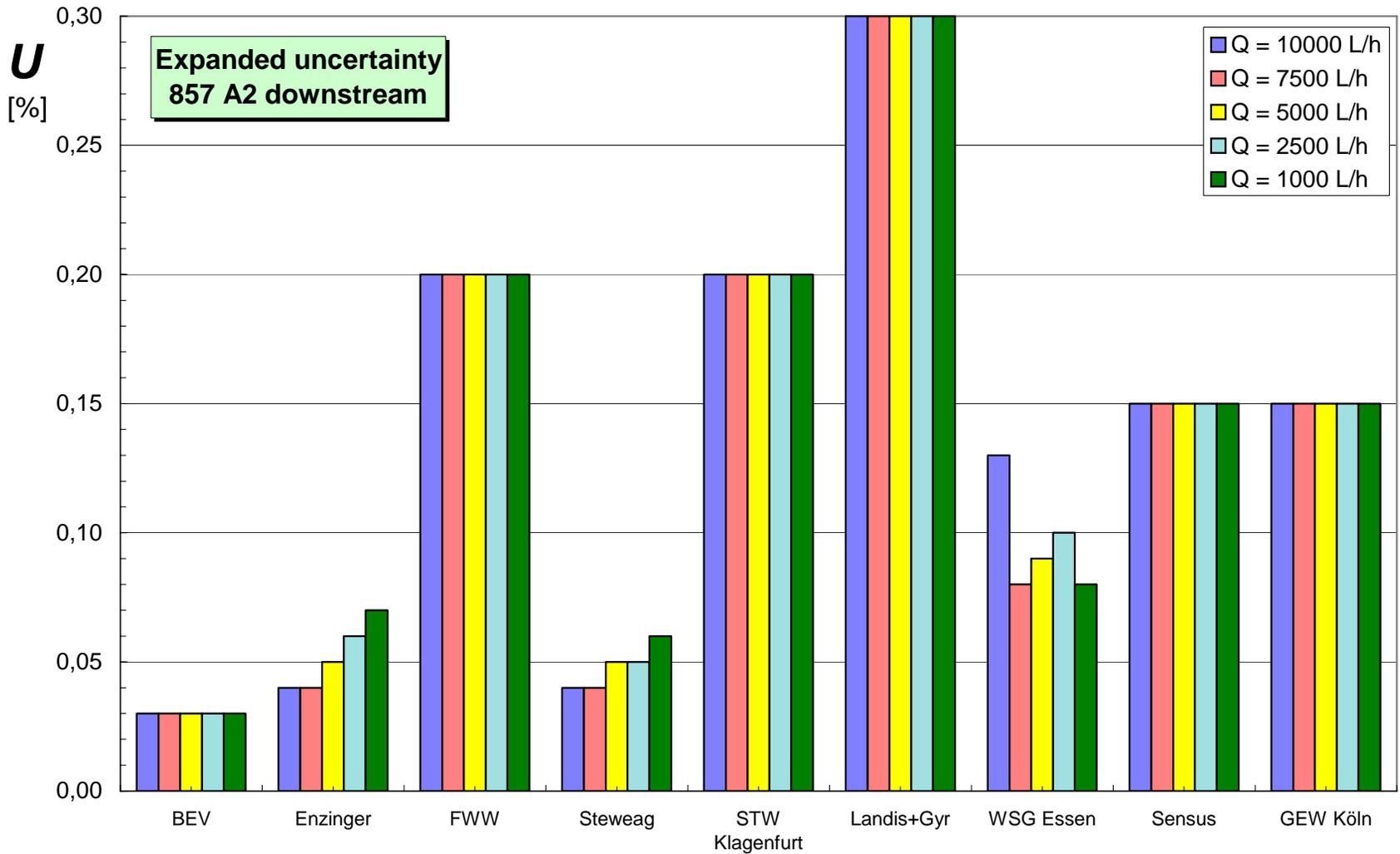




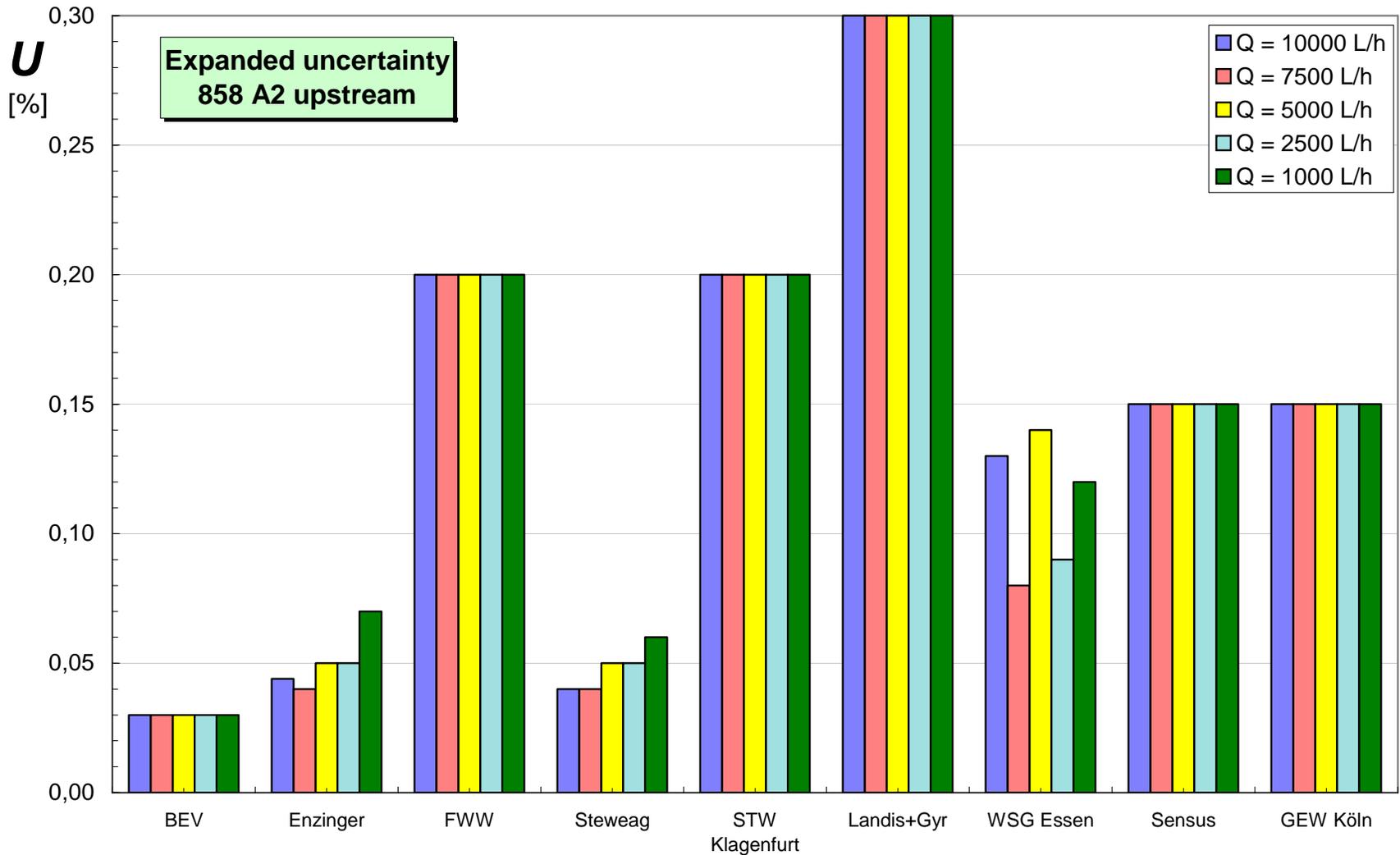
**857 - upstream**

**U**  
 [%]

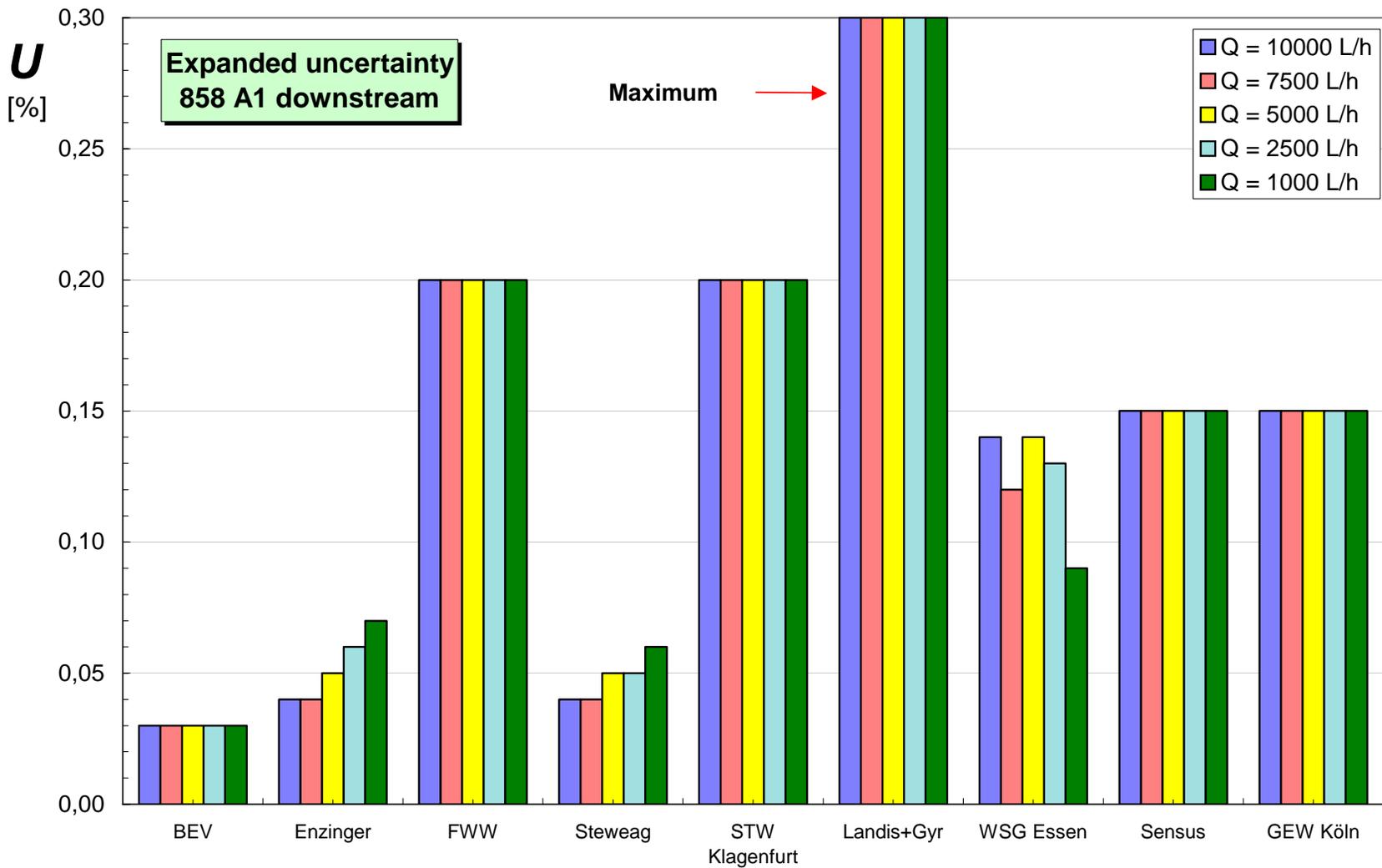




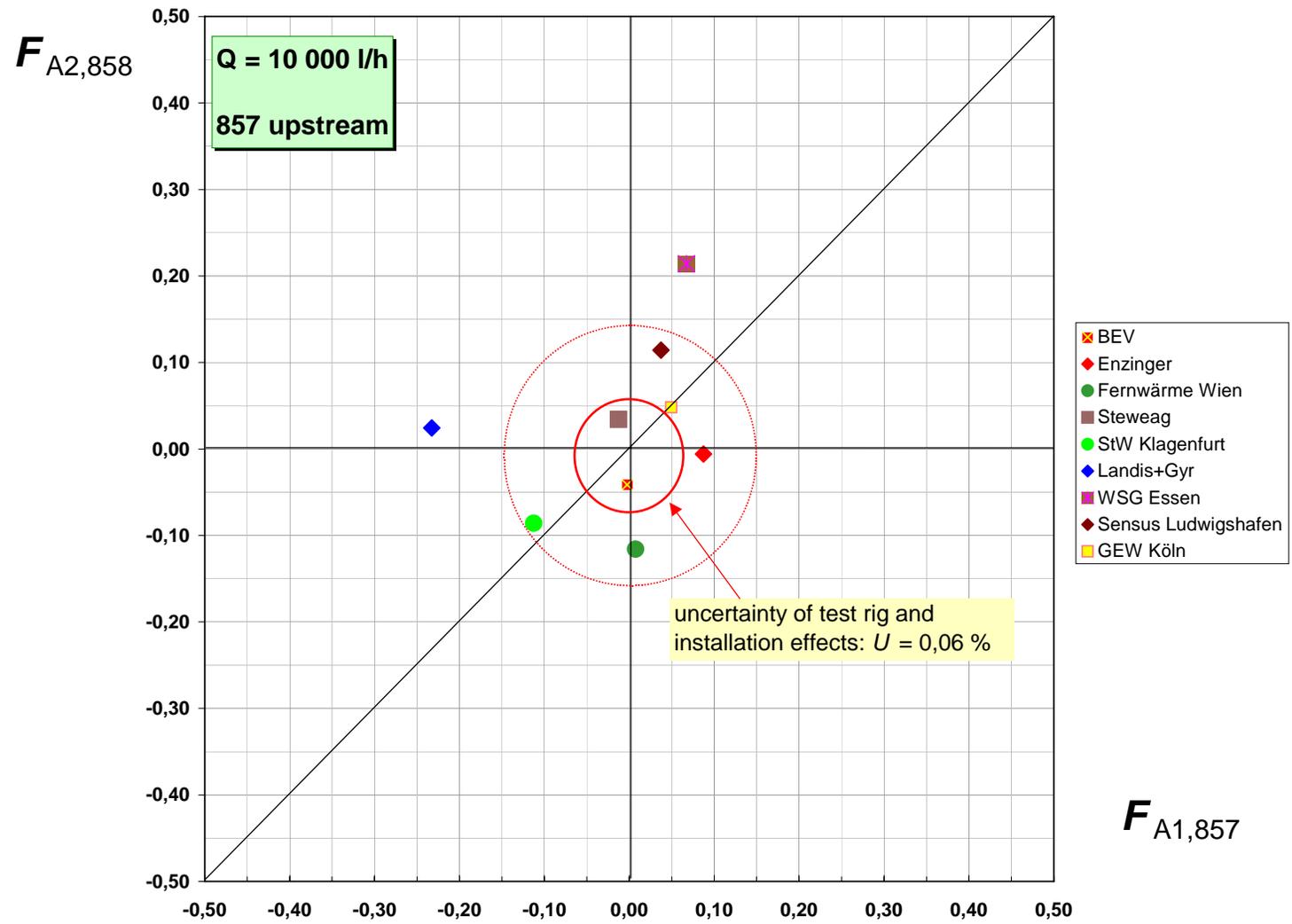
**858 - upstream**



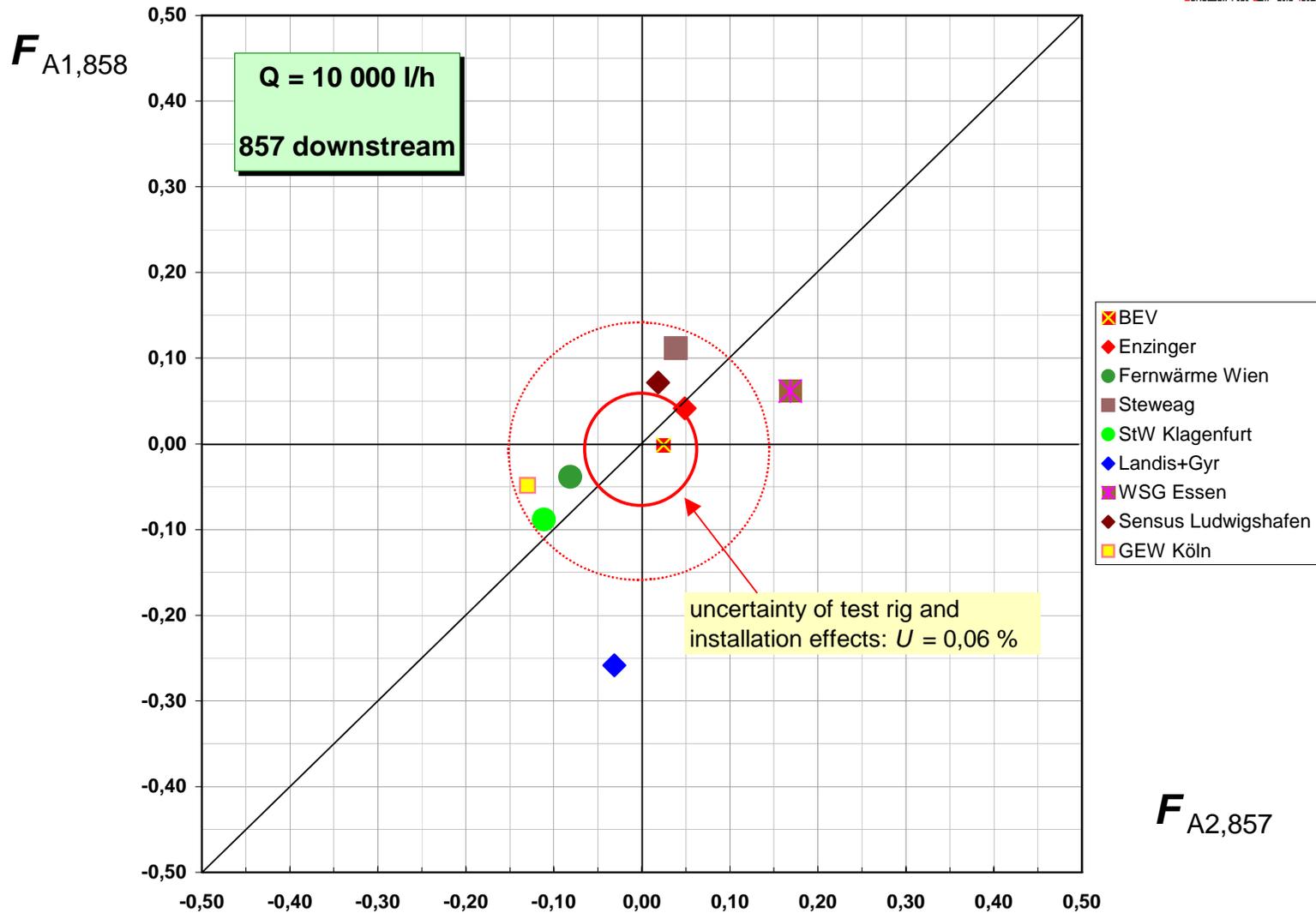
**858 - downstream**



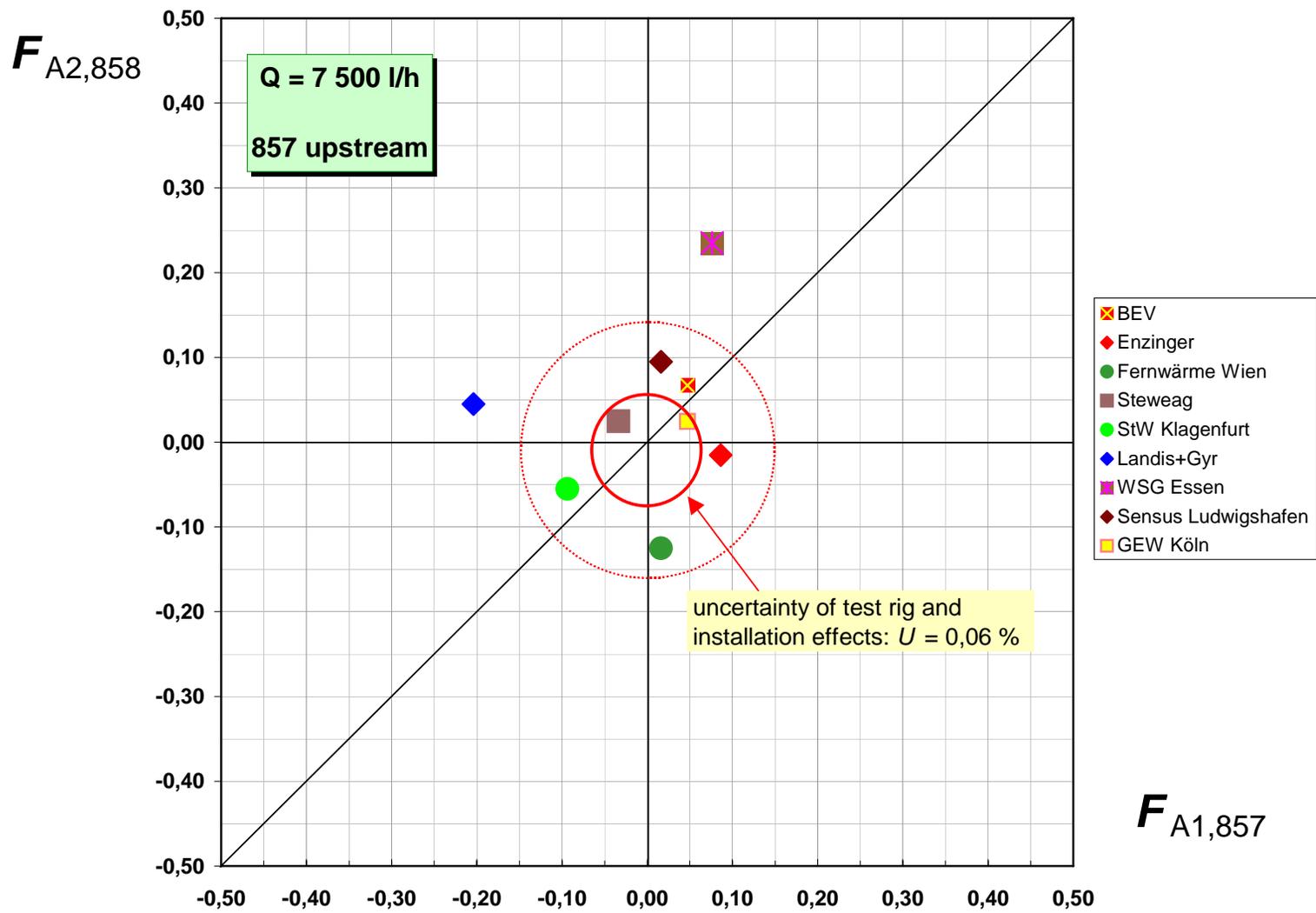
# Youdenplot 10.000 l/h



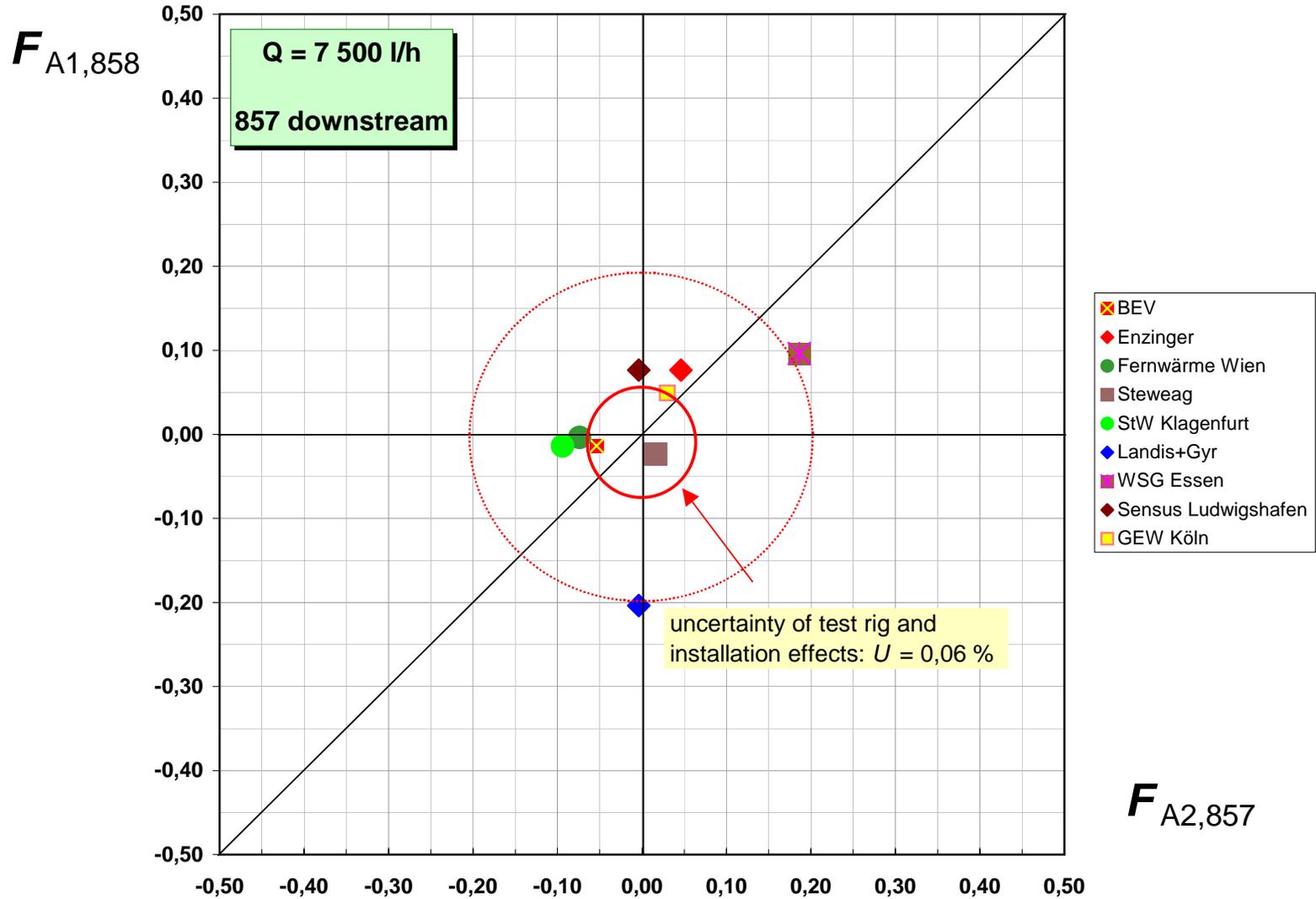
# Youdenplot 10.000 l/h



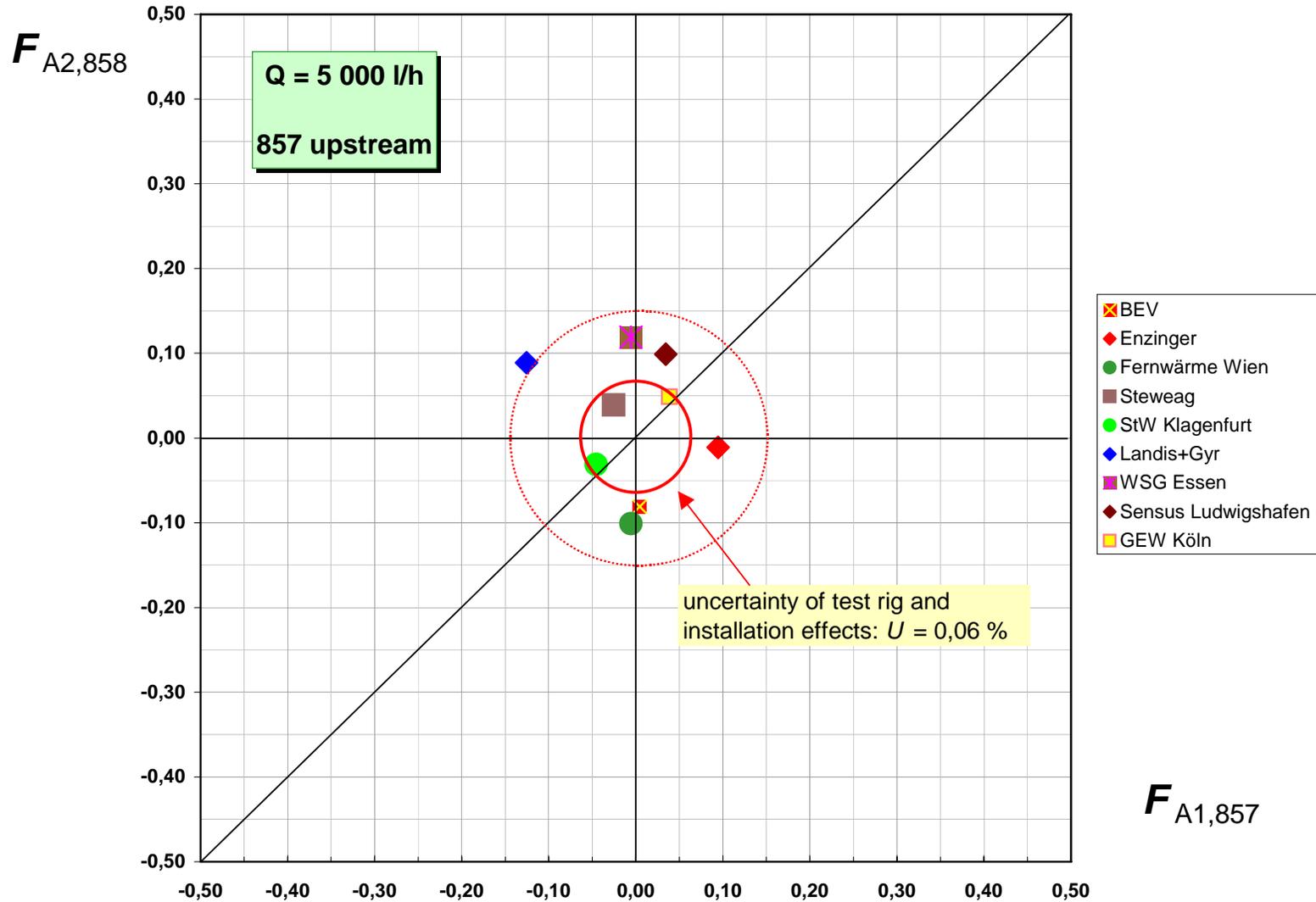
# Youdenplot 7.500 l/h



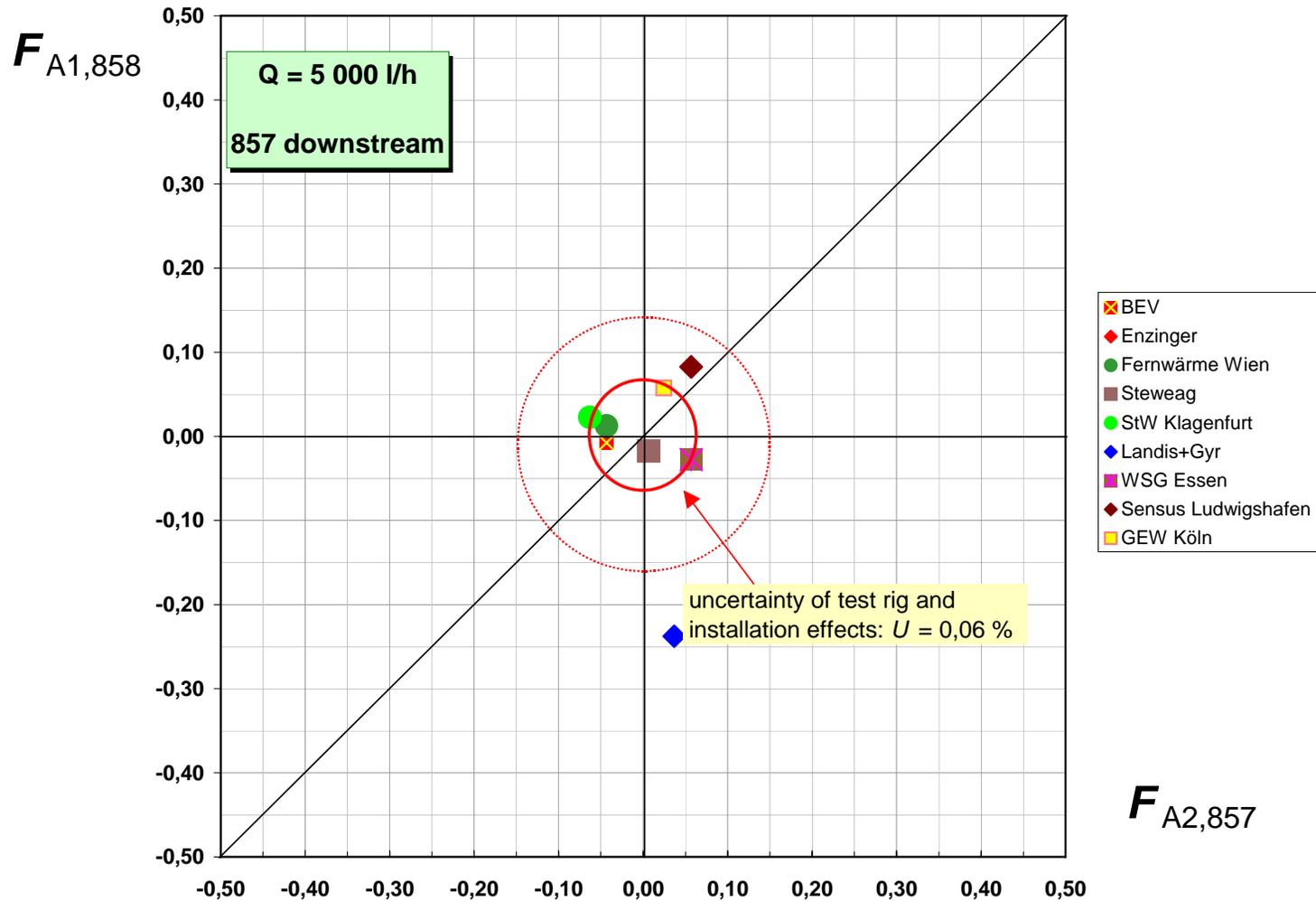
# Youdenplot 7.500 l/h



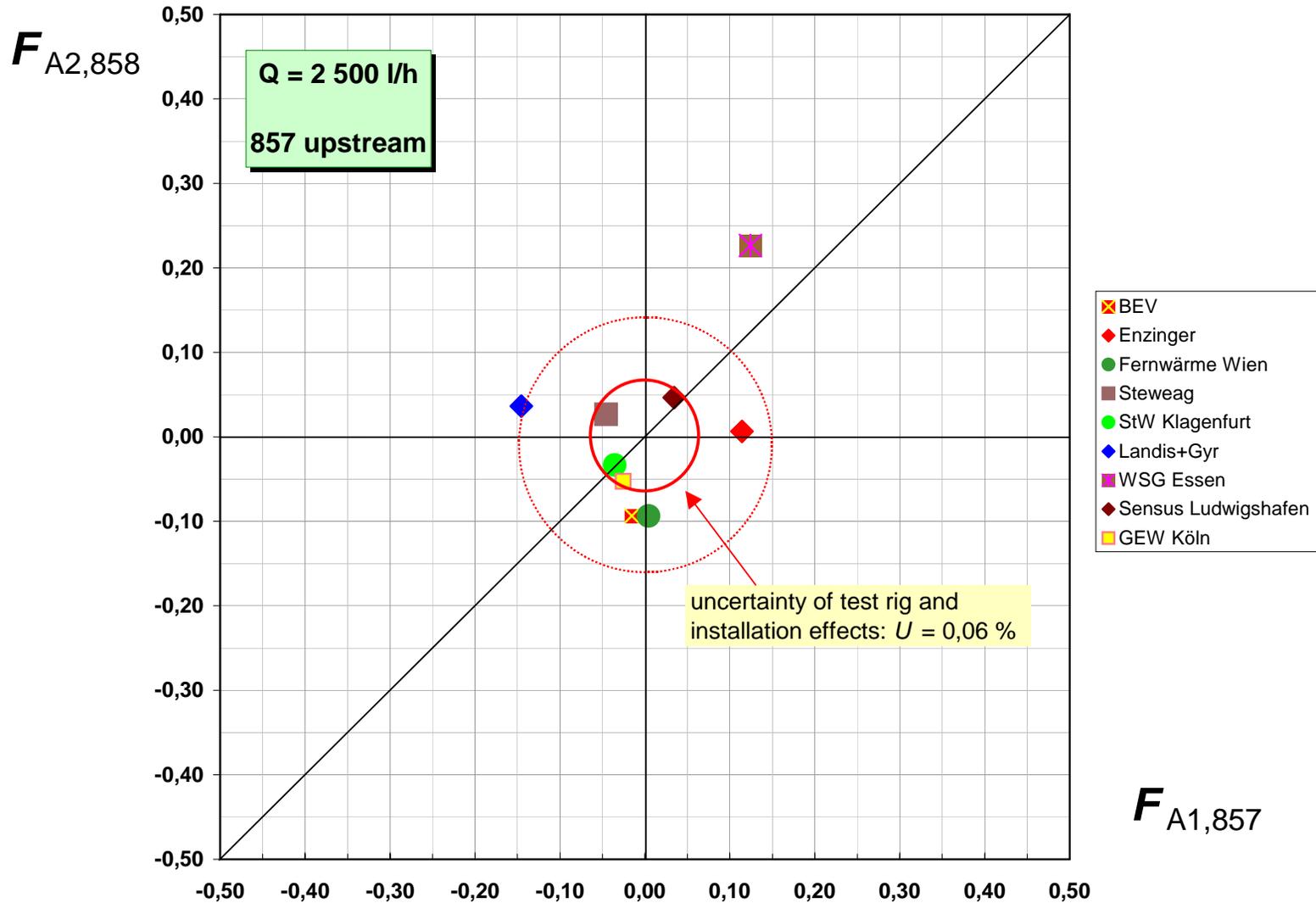
# Youdenplot 5.000 l/h



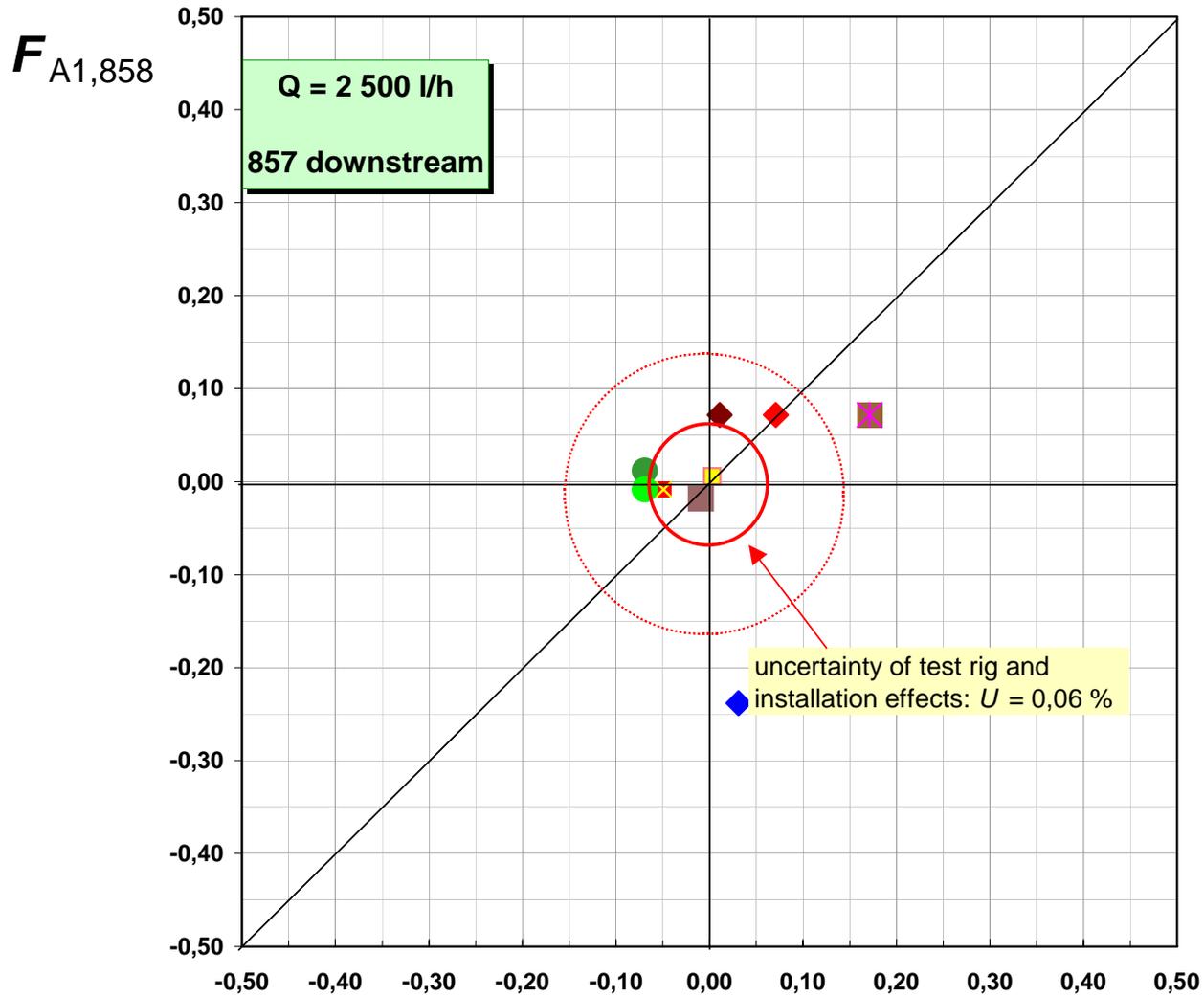
# Youdenplot 5.000 l/h



# Youdenplot 2.500 l/h

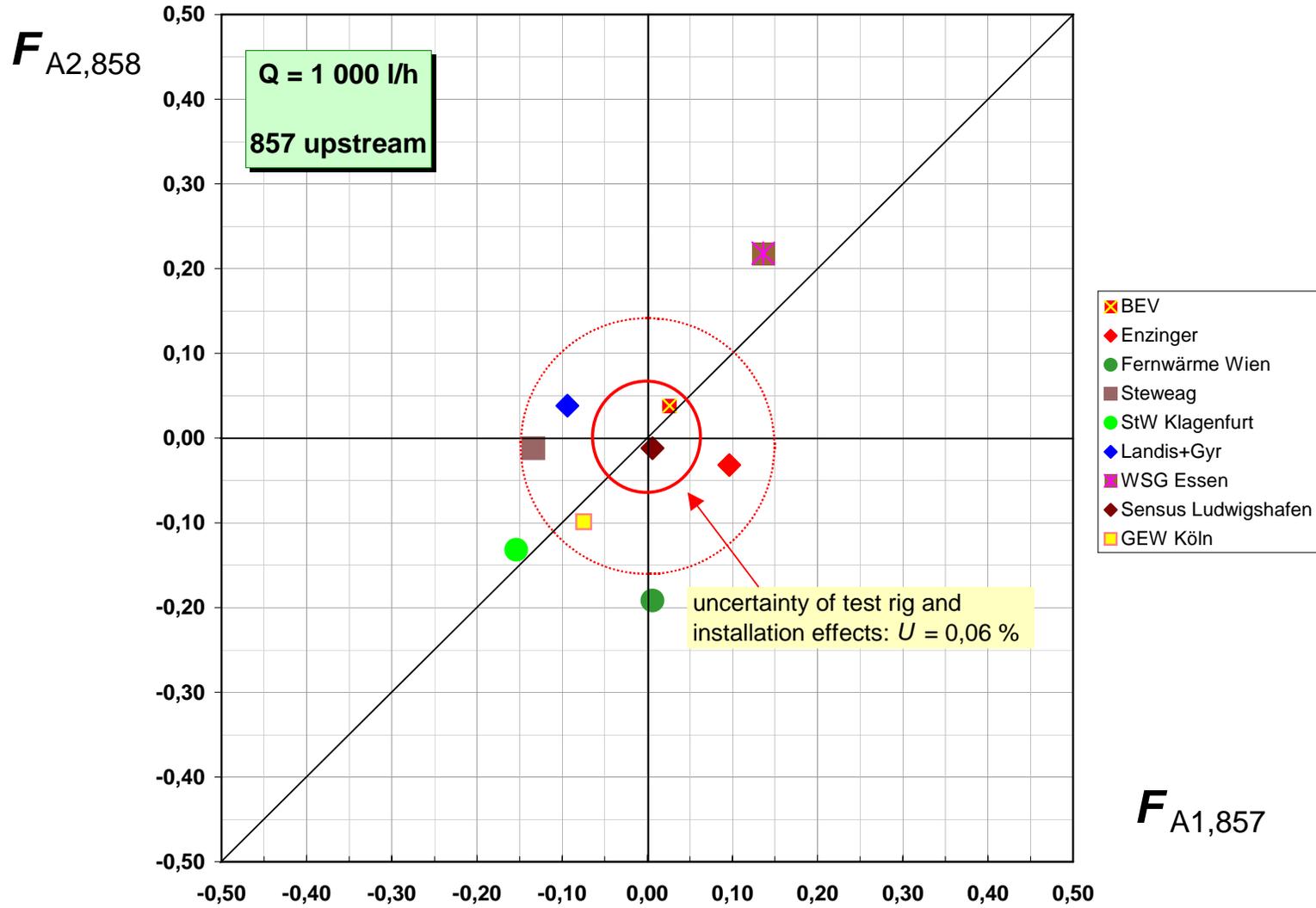


# Youdenplot 2.500 l/h



- ✘ BEV
- ◆ Enzinger
- Fernwärme Wien
- Steweag
- StW Klagenfurt
- ◆ Landis+Gyr
- ✘ WSG Essen
- ◆ Sensus Ludwigshafen
- GEW Köln

# Youdenplot 1.000 l/h



# Youdenplot 1.000 l/h

